

Strategic Managerial Incentives Arising From Product Market Competition*

Jose M. Plehn-Dujowich[†] Konstantinos Serfes[‡]

September 21, 2010

*We would like to thank workshop participants at Temple University, INSEAD, Dartmouth, the 2010 International Industrial Organization Conference (IIOC), the 2010 European Association for Research in Industrial Economics (EARIE) Annual Conference, Jaesoo Kim, and Timothy Van Zandt for very helpful comments. We are responsible for any errors.

[†]Corresponding author. Fox School of Business, Temple University, 451 Alter Hall, Philadelphia, PA 19122. E-Mail: jplehn@temple.edu. Phone: (215) 204-8139. Fax: (215) 204-5587.

[‡]Department of Economics and International Business, Bennett S. LeBow College of Business, Drexel University, Matheson Hall, 32nd and Market Streets, Philadelphia PA 19104. E-mail: ks346@drexel.edu. Phone: (215) 895-6816. Fax: (215) 895-6975.

Abstract: We develop a model in which, first, firms design compensation schemes for their managers while subject to moral hazard and, second, firms compete in Bertrand or Cournot fashion in the product market. We derive the strategic properties of managerial compensation levels and incentives. We show that the implications include: greater systematic risk may weaken the incentives of one firm while strengthening those of a competitor; an increase in the idiosyncratic risk of a firm causes all its competitors to adjust their incentives; and strategic considerations may account for the rise in U.S. CEO pay and the use of incentives.

1 Introduction

Should a manager's compensation scheme be influenced by that of a competitor's manager? If so, what are the implications for performance evaluation? We demonstrate that, due to product market competition, managerial compensation levels and incentives across firms in an industry are strategically related. Consequently, we show that a change in the corporate environment has two effects: a *direct* effect that arises due to the standard agency problem (Holmstrom 1979; Banker and Datar 1989; Bushman and Indjejikian 1993; Feltham and Xie 1994; Datar, Kulp, and Lambert 2001; Sung 2005; Dutta 2008); and a *strategic* effect which takes into account the strategic manner in which firms respond to one another. This results in novel implications about the properties of managerial compensation schemes: a reversal may occur in the conventional wisdom about risk and incentives; changes in the corporate environment of a firm cause *all* firms in the industry to adjust their compensation schemes; and a *ratcheting* effect of compensation levels and incentives may occur in response to changes in the corporate environment common to all firms in the industry, such as systematic risk.

We study an industry composed of two heterogeneous firms that are engaged in strategic product market competition (Bertrand or Cournot). Each risk-neutral firm (principal) hires a risk-averse manager (agent) to operate the firm. The marginal cost of production of a firm is a function of the effort exerted by its manager, a firm-specific shock which captures idiosyncratic risk, and an industry-wide shock which captures systematic risk. Following Raith (2003), firms reward their managers on the basis of the extent to which they reduce costs of production. We show there are countervailing effects determining the strategic properties of managerial incentives. To characterize those properties and implications thereof, we derive reasonable conditions under which managerial incentives are strategic complements or substitutes.¹ These conditions relate to the type of competition in the product market, the

¹Strategic variables have the following taxonomy (Fudenberg and Tirole 1984; Bulow, Geanakoplos, and Klemperer 1985): they are *strategic complements* if an aggressive move by one firm engenders aggressive moves by its rivals (in our context, if a firm strengthens its incentives, its rival responds by strengthening its

demand for the product, and the properties of the strategic variables being used by firms when competing in the product market.² If demand is linear and additively separable, then managerial incentives inherit the properties of the strategic variables (prices or quantities, depending on the type of competition). If firms operate in a perfectly competitive market, then managerial incentives are solely determined by the usual trade-off between risk sharing and the provision of incentives.

The manner in which managerial incentives respond to a change in the corporate environment may be decomposed into *direct* and *strategic* effects. The direct effect represents a firm's response holding fixed its rival's incentives, while the strategic effect represents a firm's reaction to the change in its rival's incentives. Thus, a large direct effect for one firm translates into a large strategic effect for its rival.

There are numerous implications stemming from the strategic nature of managerial incentives arising from product market competition. Consider the common wisdom originating from Holmstrom (1979) and Banker and Datar (1989) that an increase in risk should be associated with a weakening of managerial incentives. We show this may no longer hold due to the strategic effect. Suppose there is an increase in systematic risk and managerial incentives are strategic substitutes. Both firms have a tendency to weaken their incentives

incentives); and they are *strategic substitutes* if an aggressive move by one firm engenders defensive moves by its rivals (in our context, if a firm strengthens its incentives, its rival responds by weakening its incentives).

²Sundaram, John, and John (1996) devise an empirical means by which to determine whether the strategic variables being used by firms in the product market are strategic substitutes or complements. Their competitive strategy measure (CSM) is the correlation between the change in a firm's profit margin (which is the change in net income over the change in net sales) and the change in its competitors' net sales (whereby all firms in the same 4-digit SIC industry are included as competitors). If CSM is negative (positive), then the strategic variables are strategic substitutes (complements, respectively). The average CSM in their sample is -0.02 (with a median of -0.02), implying that their average sample firm competes on the basis of strategic substitutes. Kedia (2006) uses the same procedure as in Sundaram, John, and John to study a sample of 656 firms distributed over 196 4-digit SIC industries during the period 1984 to 1991. Kedia finds that 29 percent of the 4-digit SIC industries in the sample do not engage in strategic interaction, 21 percent compete with only strategic complements, and 21 percent compete with only strategic substitutes, while the remainder compete with combinations of strategic complements and substitutes. Overall, Kedia finds that industries with competition in prices among differentiated goods are more likely to compete in strategic complements; industries where firms compete in market share and where substantial investment is required in plant and equipment are more likely to compete in strategic substitutes; and industries with no strategic interaction are likely to be those with a large number of small firms, and those with low entry and exit barriers, suggesting they are perfectly competitive.

due to risk-sharing considerations (the direct effect). However, because managerial incentives are strategic substitutes, if a firm weakens its incentives, its rival has a tendency to respond by strengthening its incentives (the strategic effect). When the strategic effect is strong enough, one firm weakens its incentives while another strengthens them. Our model therefore provides a potential novel explanation as to why the relationship between risk and incentives is ambiguous in the empirical literature. As emphasized by Prendergast (2002), some empirical studies find that the link is positive (Core and Guay 1999; Oyer and Schaefer 2005; Rajgopal, Shevlin, and Zamora 2006); some find that the link is insignificant (Garen 1994; Yermack 1995; Bushman, Indjejikian, and Smith 1996; Ittner, Larcker, and Rajan 1997; Conyon and Murphy 2000); and others find that the link is negative (Lambert and Larcker 1987; Aggarwal and Samwick 1999a; Jin 2002).

Another implication of the strategic nature of managerial incentives is that all firms in the industry react to changes in the corporate environment that should otherwise just affect one firm. For example, consider an increase in the idiosyncratic risk of a firm, which causes the firm to weaken the incentives of its manager (as in a standard agency model); if managerial incentives are strategic complements, then the rival responds by also weakening the incentives of its manager. Therefore, firms may be adapting their compensation schemes not because of a change in their own environment, but because their competitors experienced a change in their corporate governance, for example.

We show in the Appendix that managerial compensation *levels* are also strategic. This has ramifications in the context of benchmarking CEO pay, which is prevalent (Bizjak, Lemmon, and Naveen 2008; Faulkender and Yang 2010).³ We argue it is optimal for a firm to take into account the compensation schemes of peer groups not just to ensure the CEO does not have an incentive to leave the firm (i.e., to satisfy the CEO's reservation utility), but also to implement the strategic mechanisms we identify.

Finally, if managerial compensation schemes are strategic complements, then a *ratcheting*

³In a random sample of 100 S&P 500 firms, Bizjak, Lemmon, and Naveen (2008) find that 96% use benchmarking in setting CEO pay.

effect occurs as compensation schemes react to changes in the corporate environment common to all firms in the industry. For example, consider a decline in systematic risk, which leads both firms to strengthen their incentives due to risk-sharing (the direct effect); since incentives are strategic complements, each firm responds to its rival by further strengthening its incentives (the strategic effect). Extrapolating these forces to a setting populated by many firms, as each firm in the industry reacts strategically to each competitor, the overall response is magnified as it permeates the entire industry. Thus, seemingly small changes in systematic risk can lead to dramatic changes in compensation levels and incentives. The same holds true for any change in the corporate environment that affects all firms in the industry, such as a recession or the enactment of Sarbanes-Oxley, for example. Hence, strategic considerations may have contributed towards the dramatic rise in U.S. CEO pay and the use of incentives (Gabaix and Landier 2008; Frydman and Saks 2010).⁴

The paper is organized as follows. Section 2 reviews the literature. Section 3 describes the setup of the model. Section 4 solves for the strategic properties of managerial incentives. Section 5 derives theoretical implications of these strategic properties, and Section 6 discusses their empirical ramifications. Section 7 concludes. An Appendix contains the proofs of all propositions and derives the strategic properties of managerial compensation levels, which parallel those of incentives.

2 Literature Review

We complement five literatures in agency theory and performance evaluation. The first literature concerns moral hazard problems in general, which are traditionally resolved by aligning the interests of managers and owners via incentive compensation (Holmstrom 1979; Banker and Datar 1989; Bushman and Indjejkian 1993; Feltham and Xie 1994; Datar et al. 2001; Sung 2005; Dutta 2008). Indeed, there is ample evidence that managers are rewarded

⁴Gabaix and Landier (2008) argue the rise in U.S. CEO pay is attributable to the increase in market capitalization. An alternative explanation is provided by the Lake Wobegon effect that no firm wants to admit having a CEO who is below average (Hayes and Schaefer 2009).

on the basis of performance measures, such as accounting numbers and market returns (e.g., Healy 1985; Lambert and Larcker 1987; Sloan 1993; Bushman et al. 1996; Ittner et al. 1997; Core and Guay 1999).

The second literature pertains to the design of compensation schemes among firms facing agency problems that are engaged in product market competition. In Raith (2003), an endogenous number of firms compete in prices along a Salop circle. In Baggs and de Bettignies (2007), two firms compete in prices at opposite ends of a Hotelling line. These models have *homogeneous (or symmetric)* firms and are devoid of the strategic considerations we explore. The closest model to ours is due to Aggarwal and Samwick (1999b), wherein two firms compete in Bertrand or Cournot fashion, which compares as follows. First, in our framework, uncertainty arises from shocks that affect the firm's cost of production, whereas in their model it is added onto the profit function of the firm without providing a microfoundation. This uncertainty is the source of risk that the principal must balance in providing managerial incentives. Second, their model is not solvable when managers exert effort, such that the results they discuss pertain to a setup in which there are no agency problems. Third, in their model, managers are risk-neutral, so the role of risk cannot be examined; whereas in our model managers are risk-averse. Finally, and most importantly, firms are symmetric in their model and the strategic considerations we identify are not addressed.

The third literature to which we are related links the severity of the agency problem to the extent of competition in the product market. Hart (1983), Scharfstein (1988), Hermalin (1992), Schmidt (1997), and Raith (2003) determine the impact of competition (often measured by the number of firms) on the provision of managerial effort. However, these papers do not enable compensation contracts to influence competition in the strategic manner that we identify. We discuss the empirical ramifications pertaining to this literature in Section 6 in the context of our model, and connect to the studies by Karuna (2007), Krishnan (2005), and others, who have tested these relationships.

The fourth literature concerns examining the broad ways in which managers should be

compensated in light of product market competition. Fershtman and Judd (1987) and Sklivas (1987) derive the extent to which the agent's compensation scheme should be made contingent on performance measures other than profit, finding that positive weight should be placed on sales due to product market competition. These models are devoid of moral hazard (or adverse selection) and risk aversion.⁵

The fifth literature shows that debt contracts influence product market competition. Bolton and Scharfstein (1990), Rotemberg and Scharfstein (1990), and Maksimovic (1988) demonstrate how capital structure changes the intensity of competition. In these models, firms initially choose their capital structure and then compete in the product market. Debt serves to commit managers to be more or less aggressive depending on parameter values. Our model provides analogous findings on the relationship between compensation contracts and product market competition.

Finally, our paper relates to a general question posed in game theory as to whether strategic substitutability or complementarity in a static framework translates into strategic substitutability or complementarity in a dynamic framework, e.g., Echenique (2004) and Vives (2009).

3 The Model

3.1 Timing and Structure of the Game

There are two firms (the principals) and two managers (the agents) in an industry.⁶ Each principal hires an agent to operate the firm, and the manager-firm pairings are labeled 1 and 2. The firms compete in Cournot or Bertrand fashion with products that are substi-

⁵See also Vickers (1985) and Katz (1991). Fumas (1992) extends this literature to include relative performance evaluation in a model similar to Aggarwal and Samwick (1999b).

⁶The literature that combines product market competition with agency problems is typically ambiguous as to exactly who constitutes the agent. The agent may be the CEO, a product line manager, or a plant manager, for example. When discussing some empirical implications of the model, we interpret the agent as the CEO.

tutes. Following Raith (2003), managerial effort e_i reduces the (constant) marginal cost of production. For $i = 1, 2$, the marginal cost of firm i is

$$c_i = c - (\theta_i + \theta)e_i - \varepsilon_i - \varepsilon, \quad (1)$$

where ε_i is a firm-specific normal shock with mean zero and variance σ_i^2 that is independent across firms, ε is a normal shock common to both firms with mean zero and variance σ^2 , and c is an industry-wide parameter (that reflects the technology of the industry).⁷ The sensitivity of marginal cost to managerial effort has a firm-specific component, θ_i , and an industry-wide component, θ .⁸ The volatility σ_i^2 measures the firm-specific (i.e., idiosyncratic) risk of firm i ; and σ^2 measures industry-wide risk, which may thus be interpreted as systematic risk. For ease of exposition, we assume that ε_i and ε are independently distributed.⁹ Both agents have the effort cost function $e_i^2/2$ and reservation utility r . As is common in the agency literature, both agents have constant absolute risk aversion (CARA) preferences with the coefficient of absolute risk aversion R .¹⁰

The timing of the game is as follows:

1. Agents are exogenously matched to principals.
2. Principals design contracts that satisfy individual rationality and incentive compatibility. The contracts are observed by the two firms.
3. Agents accept or reject the contracts and exert unobservable effort if they accept.

⁷Because the shock distributions are normal, with positive probability there is an arbitrarily high realization of the shocks that yields a negative marginal cost. Raith (2003) provides explicit conditions on the parameters of the shock distribution (mean and variance) which guarantee that this probability is arbitrarily small. Given the generality of our demand system, however, we cannot provide a similar explicit condition, but nevertheless it is clear that if we assume the standard deviations are sufficiently small, then the probability of a negative realized marginal cost is practically zero.

⁸The common factor θ may reflect the stage of the industry's life cycle, for example: when the industry is young, there are many opportunities to experience efficiency gains via learning (in which case θ is large); but when the industry is mature, most learning has already taken place, so there are few opportunities remaining to cut costs (in which case θ is small).

⁹The analysis does not change if firm-specific and industry-wide risks are correlated.

¹⁰The analysis does not change if the agents have heterogeneous costs of effort, reservation utilities, and risk aversion parameters.

4. Firms engage in Cournot or Bertrand competition.¹¹
5. Shocks (and thereby costs of production) are realized and agents are compensated.

We solve the game using backwards induction as follows. First, we derive the manager's optimal effort policy as a function of the incentives he is offered by the firm. Second, we derive the Nash equilibrium prices or quantities as a function of managerial incentives. Third, we solve the principal's problem, which entails choosing the compensation scheme of the manager that maximizes firm profit subject to the conditions that the manager signs the contract (individual rationality) and exerts the desired level of effort (incentive compatibility). In designing its compensation scheme, each firm anticipates that the strength of the incentives offered its manager affects not just its optimal price or quantity policy, but also that of its rival.

3.2 The Manager's Effort Problem

This stage of the game is the same regardless of the type of product market competition (Bertrand or Cournot). Following Raith (2003), the principal compensates the agent according to the extent to which he reduces the firm's marginal cost of production. Specifically, the contract takes the linear form

$$t_i = \alpha_i + \beta_i(c - c_i), \tag{2}$$

where α_i represents the agent's salary and β_i the agent's incentives. Let $\beta = (\beta_1, \beta_2)$ denote the vector of managerial incentives. The term $c - c_i = (\theta_i + \theta)e_i + \varepsilon_i + \varepsilon$ is the performance measure by which the manager is evaluated. Thus, firms potentially differ along two dimensions: the precision of the performance measure $1/(\sigma_i^2 + \sigma^2)$; and the sensitivity of marginal cost to managerial effort $\theta_i + \theta$.

¹¹We presume in our exposition that the firms make the pricing or quantity decisions. However, the managers would make the same choices.

Making the manager's compensation contingent on the extent of the cost reduction is informationally efficient given that effort reduces cost (Holmstrom 1979). A drawback of our framework is that it favors the usage of relative performance evaluation (RPE). Since firms are subject to industry-wide (or systematic) risk ε , the marginal costs of production are correlated across firms. Therefore, it would be beneficial for the principal to contract on the marginal cost of the rival since it is informative. Raith does not require the usage of RPE because firms are only subject to idiosyncratic risk. Other agency models with product market competition, such as Aggarwal and Samwick (1999b) and Baggs and de Bettignies (2007), require RPE. Most papers suggest there is little evidence of RPE (Aggarwal and Samwick 1999b; Antle and Smith 1986; Janakiraman et al. 1992), but some recent evidence favors RPE (Albuquerque 2009). Oyer (2004) shows that the absence of RPE is optimal if the reservation utility of an agent varies with the business cycle; Bizjak et al. (2008) and Rajgopal et al. (2006) find evidence consistent with this hypothesis.

The certainty equivalent of agent i is

$$CE_i = \alpha_i + \beta_i(\theta_i + \theta)e_i - R\beta_i^2(\sigma_i^2 + \sigma^2)/2 - e_i^2/2. \quad (3)$$

This yields the effort policy

$$e_i = \beta_i(\theta_i + \theta), \quad (4)$$

such that the expected marginal cost of firm i is given by

$$E(c_i) = c - \beta_i(\theta_i + \theta)^2. \quad (5)$$

The stronger are managerial incentives, the smaller is the firm's (expected) marginal cost of production. By virtue of our timing structure, expected profits and optimal prices or quantities only depend on expected costs.

3.3 Product Market Demand

Following Singh and Vives (1984), suppose that $U(q_1, q_2)$ is a strictly concave and strictly monotone utility function representing the preferences of a representative consumer. Let $q = (q_1, q_2)$ and $p = (p_1, p_2)$ denote the vector of quantities and prices, respectively. The representative consumer maximizes $U(q) - pq$, which gives rise to an inverse demand system $p_i = d_i(q)$. Inverse demand functions are downward sloping, $\partial d_i / \partial q_i < 0$, and the cross effects, $\partial d_i / \partial q_j$, are negative because the goods are substitutes. The inverse demand system can be inverted to yield a direct demand system $q_i = D_i(p)$.¹² Direct demand functions are downward sloping, $\partial D_i / \partial p_i < 0$, and $\partial D_i / \partial p_j$ is positive since the products are substitutes. Furthermore, we assume that the “own effect” $|\partial D_i / \partial p_i|$ or $|\partial d_i / \partial q_i|$ is larger than the “cross effect” $|\partial D_i / \partial p_j|$ or $|\partial d_i / \partial q_j|$. The expected gross profit of firm i in terms of prices is

$$\pi_i(p) = (p_i - (c - \beta_i(\theta_i + \theta)^2)) D_i(p); \quad (6)$$

and in terms of quantities is

$$\hat{\pi}_i(q) = (d_i(q) - (c - \beta_i(\theta_i + \theta)^2)) q_i. \quad (7)$$

To ensure second-order conditions are satisfied, we assume that expected gross profit functions are strictly concave in their own strategic variable:

Assumption 1 (Concavity)

$$\frac{\partial^2 \pi_i}{\partial p_i^2} < 0 \text{ for all } p \text{ and } \frac{\partial^2 \hat{\pi}_i}{\partial q_i^2} < 0 \text{ for all } q.$$

We make the following assumptions to ensure that reaction functions in the product market are well-behaved and have slopes less than one in absolute value so as to obtain a

¹²We assume that demand is satiated; that is, when the price is zero, quantity demanded is finite. This is true, for example, when the demand system is linear.

unique price or quantity Nash equilibrium:

Assumption 2 (Stability and Uniqueness)

$$\frac{\partial^2 \pi_i}{\partial p_i^2} + \left| \frac{\partial^2 \pi_i}{\partial p_i \partial p_j} \right| < 0 \text{ for all } p \text{ and } \frac{\partial^2 \hat{\pi}_i}{\partial q_i^2} + \left| \frac{\partial^2 \hat{\pi}_i}{\partial q_i \partial q_j} \right| < 0 \text{ for all } q.$$

We assume prices are strategic complements and quantities are strategic substitutes.¹³

Assumption 3 (Strategic Substitutability and Complementarity)

$$\frac{\partial^2 \pi_i}{\partial p_i \partial p_j} > 0 \text{ for all } p \text{ and } \frac{\partial^2 \hat{\pi}_i}{\partial q_i \partial q_j} < 0 \text{ for all } q.$$

We introduce the following definitions. As stated earlier, the products sold by the two firms are substitutes, implying $\partial \pi_i / \partial p_j > 0$ and $\partial \hat{\pi}_i / \partial q_j < 0$. In the context of Bertrand competition, we say that if an increase in the rival's price raises the firm's profit at an increasing rate, then the products exhibit *increasing substitutability*, i.e. $\partial^2 \pi_i / \partial p_j^2 \geq 0$; and if it does so at a decreasing rate, then they exhibit *decreasing substitutability*, i.e. $\partial^2 \pi_i / \partial p_j^2 \leq 0$.¹⁴ For increasing (decreasing) substitutability, we need a demand function that is convex (concave, respectively) in the rival's price, i.e., $\partial^2 D_i / \partial p_j^2 \geq (\leq) 0$. If demand is linear in the rival's price, then the effect is absent, such that $\partial^2 \pi_i / \partial p_j^2 = 0$. Decreasing substitutability arises if demand is derived from a CES utility with an elasticity of substitution between 1 and 2, while increasing substitutability arises with an elasticity of substitution in excess of 2, for example.

Finally, we say that the demand function $D_i(p)$ exhibits *supermodularity (submodularity)* with respect to prices if $\partial^2 D_i / (\partial p_i \partial p_j) \geq (\leq) 0$. This affects the strength of strategic complementarity $\partial^2 \pi_i / (\partial p_i \partial p_j)$ with respect to marginal cost since $\partial^2 \pi_i / (\partial p_i \partial p_j) =$

¹³With linear demand, it is always the case that prices are strategic complements and quantities are strategic substitutes when the products are substitutes.

¹⁴Similarly, in the context of Cournot competition, we say that if an increase in the rival's quantity decreases the firm's profit at an increasing rate, then the products exhibit *increasing substitutability*, i.e. $\partial^2 \hat{\pi}_i / \partial q_j^2 \leq 0$; and if it does so at a decreasing rate, then they exhibit *decreasing substitutability*, i.e. $\partial^2 \hat{\pi}_i / \partial q_j^2 \geq 0$.

$(p_i - c_i)\partial^2 D_i / (\partial p_i \partial p_j) + \partial D_i / \partial p_j$. A lower marginal cost c_i (due to stronger incentives β_i) makes the degree of strategic complementarity stronger if and only if demand is supermodular with respect to prices. Intuitively, an increase in the rival's price benefits the firm; with supermodularity (submodularity), the higher is the firm's price, the more (less, respectively) the firm benefits from the increase in the rival's price. If demand is additively separable, then the effect disappears, such that $\partial^2 D_i / (\partial p_i \partial p_j) = 0$.

4 Strategic Managerial Incentives

4.1 Bertrand Competition in the Product Market

Firm i maximizes expected gross profit $\pi_i(p) = (p_i - (c - \beta_i(\theta_i + \theta)^2)) D_i(p)$ with respect to its price p_i to yield the first-order condition (FOC)

$$\frac{\partial \pi_i}{\partial p_i} = (p_i - (c - \beta_i(\theta_i + \theta)^2)) \frac{\partial D_i}{\partial p_i} + D_i(p) = 0. \quad (8)$$

The second-order condition (SOC) is satisfied by virtue of Assumption 1. We denote the unique price equilibrium by $\{p_1^*(\beta), p_2^*(\beta)\}$. Let $\pi_i(p_i^*(\beta), p_j^*(\beta), \beta_i)$ denote the gross profit of firm i at the optimum. We discuss below the three mechanisms by which the managerial incentives offered to manager i influence the gross profit of firm i .

The following lemma derives the manner in which managerial incentives affect equilibrium prices:

Lemma 1 (Incentives and Prices with Bertrand Competition) *The equilibrium price of firm i is decreasing in the incentives of its manager and the incentives of its rival's manager, i.e. $\partial p_i^* / \partial \beta_i < 0$ and $\partial p_i^* / \partial \beta_j < 0$.*

Suppose firm i strengthens the incentives of its manager. This spurs the manager of firm i to exert greater effort, which lowers the firm's expected marginal cost and thereby

leads the firm to charge a lower price for its product, i.e. $\partial p_i^*/\partial \beta_i < 0$. Given the strategic complementarity of prices, the rival responds by lowering its price, $\partial p_j^*/\partial \beta_i < 0$.

We now derive the equilibrium set of managerial incentives. The principal associated with firm i maximizes the firm's net profit (i.e., net of the agent's expected total compensation)

$$\max_{\{\alpha_i^B, \beta_i^B, e_i^B\}} \pi_i^B - E(t_i^B), \quad (9)$$

subject to the individual rationality (IR) constraint of the agent:

$$\alpha_i^B + \beta_i^B(\theta_i + \theta)e_i^B - R(\beta_i^B)^2(\sigma_i^2 + \sigma^2)/2 - (e_i^B)^2/2 \geq r, \quad (10)$$

and the incentive compatibility (IC) constraint of the agent given by the effort policy $e_i^B = \beta_i^B(\theta_i + \theta)$. The IR constraint binds at the optimum, yielding the expected total compensation $E(t_i^B) = r + R(\beta_i^B)^2(\sigma_i^2 + \sigma^2)/2 + (e_i^B)^2/2$. Applying the effort policy, the expected total compensation of the agent becomes

$$E(t_i^B) = r + (\beta_i^B)^2[(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)]/2. \quad (11)$$

The principal's net profit thereby becomes

$$\begin{aligned} \pi_i^B - E(t_i^B) &= (p_i^*(\beta^B) - (c - \beta_i^B(\theta_i + \theta)^2)) D_i(p^*(\beta^B)) - E(t_i^B) \\ &= \pi_i^B(p_i^*(\beta^B), p_j^*(\beta^B), \beta_i^B) - (\beta_i^B)^2[(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)]/2 - r. \end{aligned} \quad (12)$$

The FOC with respect to β_i^B yields

$$\frac{\partial (\pi_i^B - E(t_i^B))}{\partial \beta_i^B} = \frac{\partial \pi_i^B}{\partial p_i^*} \frac{\partial p_i^*}{\partial \beta_i^B} + \frac{\partial \pi_i^B}{\partial p_j^*} \frac{\partial p_j^*}{\partial \beta_i^B} + \frac{\partial \pi_i^B}{\partial \beta_i^B} - \beta_i^B[(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)] = 0. \quad (13)$$

The incentives of the manager affect the principal's net profit through four different channels. The first two operate via the product market by influencing the firm's and rival's

prices, while the latter two arise in an isolated principal-agent problem (i.e., they represent the usual trade-off between risk-sharing and incentives). First, there is the term $\frac{\partial \pi_i^B}{\partial p_i^*} \frac{\partial p_i^*}{\partial \beta_i^B}$, which captures the extent to which the gross profit of the firm is influenced by the impact of managerial incentives on its own price. Because the firm chooses in a later stage of the game the price that maximizes its gross profit, this effect, by the envelope theorem, disappears. Second, there is the term $\frac{\partial \pi_i^B}{\partial p_j^*} \frac{\partial p_j^*}{\partial \beta_i^B}$, which captures the extent to which the gross profit of the firm is influenced by the impact of managerial incentives on its rival's price. We label this the *strategic effect*, which arises because $\partial p_i^* / \partial \beta_j^B \neq 0$, following from the fact that $\partial^2 \pi_i^B / \partial p_j^* \partial p_i^* \neq 0$. The strategic effect is negative: when firm i offers stronger incentives to its manager, the rival's price decreases ($\partial p_j^* / \partial \beta_i^B < 0$) by Lemma 1 because prices are strategic complements, which leads to a decline in firm i 's gross profit ($\partial \pi_i^B / \partial p_j^* > 0$) since the products are substitutes. Third, there is the term $\partial \pi_i^B / \partial \beta_i^B > 0$, which measures the extent to which the manager's effort reduces the firm's expected marginal cost. Fourth, there is the term $-\beta_i^B [(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)]$: an increase in incentives induces greater effort and exposes the risk-averse agent to more risk, both of which cause the principal to enhance the agent's expected total compensation. Overall, the benefit from strengthening incentives originates from the reduction in marginal cost, while the cost is manifested via the (negative) strategic effect and increased compensation.

The managerial incentives of firm i respond to a change in the managerial incentives of

Lemma 1, and in particular equation (22), from which we infer

$$\frac{\partial^2 p_j^*}{\partial \beta_i \partial \beta_j} = \frac{1}{\Delta} \left((\theta_j + \theta)^2 \frac{\partial^2 D_j}{\partial p_i \partial p_j} \right) \frac{\partial D_i}{\partial p_i} (\theta_i + \theta)^2, \quad (15)$$

where $\Delta \equiv \frac{\partial^2 \pi_1}{\partial p_1^2} \frac{\partial^2 \pi_2}{\partial p_2^2} - \frac{\partial^2 \pi_1}{\partial p_1 \partial p_2} \frac{\partial^2 \pi_2}{\partial p_2 \partial p_1}$. If demand is supermodular, then $\partial^2 p_j^* / (\partial \beta_i \partial \beta_j) \leq 0$ given that $\Delta > 0$ from Assumption 2 and $\partial D_i / \partial p_i < 0$, implying that an increase in β_j leads to a higher $|\partial p_j / \partial \beta_i|$ (recall that this term is negative). This hurts firm i 's profit more, inducing firm i to respond by weakening its incentives β_i in order to mitigate this negative effect. If, on the other hand, demand is submodular, then firm i responds by strengthening its incentives. Therefore, the second effect operates in the same direction as the first effect if demand is submodular. The second effect is absent if demand is additively separable.

Third, when firm i becomes more aggressive, it triggers an even more aggressive response on the part of firm j in the pricing stage of the game. This hurts firm i 's profit when demand exhibits decreasing substitutability. To see this, note that the profit of firm i is increasing in the price of its rival p_j , and, under decreasing substitutability, it is concave in p_j . The strategic effect in this case becomes more negative when firm j strengthens its incentives β_j .¹⁵ Firm i loses more by strengthening its incentives, so it lowers β_i . This third effect, which is captured by the third term in the numerator of (14), operates in the opposite direction from the first effect. Under increasing substitutability, however, both effects operate in the same direction. This third effect is absent if demand is linear in the rival's price.

To summarize, if demand functions exhibit strong supermodularity and decreasing substitutability, relative to the effect of strategic complementarity, then the second and third terms in the numerator of (14) dominate the first term, such that managerial incentives are strategic substitutes, i.e., $d\beta_i^B / d\beta_j^B < 0$. On the other hand, if demand functions exhibit submodularity and increasing or weakly decreasing substitutability, all three effects point in the same direction, such that managerial incentives are strategic complements, i.e.,

¹⁵That is, p_j moves down the concave profit function, so the slope increases.

$d\beta_i^B/d\beta_j^B > 0$. The next proposition states our findings.¹⁶

Proposition 1 (Strategic Incentives with Bertrand Competition) *Managerial incentives are strategic substitutes if demand functions exhibit strong supermodularity and decreasing substitutability; and they are strategic complements if demand functions exhibit submodularity and increasing or weakly decreasing substitutability.*

If demand is linear and additively separable in prices (e.g., $D_i = A - p_i + \gamma p_j$), then only the first term in the numerator of (14) remains (the other two become zero), such that incentives are strategic complements (as are prices). In other words, in this case, managerial incentives inherit the properties of the strategic variables (prices) being utilized by firms when competing in the product market.

Moreover, if firms operate in a perfectly competitive market, then their actions (prices) are no longer strategic; that is, firms are price-takers. In this case, managerial incentives are no longer strategic, such that $d\beta_i^B/d\beta_j^B = 0$ (since we have that $\frac{\partial^2 \pi_i^B}{\partial p_i^* \partial p_i^*} = 0$ and $\frac{\partial^2 \pi_i^B}{\partial (p_i^*)^2} = 0$).

The distinction between an agent's reservation utility r and compensation scheme (α_i, β_i) are important. Irrespective of the strategic properties of managerial incentives, it is always the case that each agent earns his reservation utility. Therefore, if a firm weakens the incentives of its manager in response to an action by its competitor, this may be accompanied by an adjustment in the manager's salary so as to ensure retention.

¹⁶Given the continuity of the principal's profit function with respect to β and the fact that β_i lies in a compact set, existence of equilibrium in stage 1 of the game is guaranteed if the principal's profit function is quasi-concave in β_i . This arises if the degree of constant relative risk aversion R and/or the variances σ^2 and σ_i^2 (which do not affect equilibrium prices p^*) are large enough; see the denominator of (14). This also implies that we have single-valued best-responses, which according to Proposition 1, slope either up or down. For a unique equilibrium $\{\beta_1^B, \beta_2^B\}$ of managerial incentives to exist, we require that $\left| \frac{d\beta_i^B}{d\beta_j^B} \right| < 1$. With linear demand, this condition holds for a wide range of parameter values, but we do not have general conditions on fundamentals that would guarantee this condition and hence uniqueness. In any case, the comparative statics we perform below in (β_1, β_2) space can be performed locally around any stable equilibrium, without changing our insights qualitatively.

4.2 Cournot Competition in the Product Market

The analysis in this sub-section parallels the scenario with Bertrand competition.¹⁷ Firm i maximizes expected gross profit $\hat{\pi}_i(q) = (d_i(q) - (c - \beta_i(\theta_i + \theta)^2))q_i$ with respect to its quantity q_i to yield the FOC

$$\frac{\partial \hat{\pi}_i}{\partial q_i} = \frac{\partial d_i}{\partial q_i} q_i + d_i(q) - (c - \beta_i(\theta_i + \theta)^2) = 0. \quad (16)$$

The SOC is satisfied by virtue of Assumption 1. We denote the unique quantity equilibrium by $\{q_1^*(\beta), q_2^*(\beta)\}$. The following lemma derives the manner in which managerial incentives affect equilibrium quantities:

Lemma 2 (Managerial Incentives and Quantities with Cournot Competition) *The equilibrium quantity of firm i is increasing in the incentives of its manager and decreasing in the incentives of its rival's manager, i.e. $\partial q_i^*/\partial \beta_i > 0$ and $\partial q_i^*/\partial \beta_j < 0$.*

The principal's objective is

$$\begin{aligned} \hat{\pi}_i^C - E(t_i^C) &= (d_i(q^*(\beta^C)) - (c - \beta_i^C(\theta_i + \theta)^2)) q_i^*(\beta^C) - E(t_i^C) \\ &= \hat{\pi}_i^C(q_i^*(\beta^C), q_j^*(\beta^C), \beta_i^C) - (\beta_i^C)^2[(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)]/2 - r. \end{aligned} \quad (17)$$

The FOC with respect to β_i^C yields

$$\frac{\partial (\hat{\pi}_i^C - E(t_i^C))}{\partial \beta_i^C} = \frac{\partial \hat{\pi}_i^C}{\partial q_i^*} \frac{\partial q_i^*}{\partial \beta_i^C} + \frac{\partial \hat{\pi}_i^C}{\partial q_j^*} \frac{\partial q_j^*}{\partial \beta_i^C} + \frac{\partial \hat{\pi}_i^C}{\partial \beta_i^C} - \beta_i^C[(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)] = 0. \quad (18)$$

¹⁷Kreps and Scheinkman (1983) study a two-stage game in which, first, firms choose capacities (that constrain how much they may produce) and, second, firms compete in prices. The authors show that, under mild assumptions about demand, the unique equilibrium outcome is the Cournot outcome.

The managerial incentives of firm i respond to a change in the managerial incentives of firm j as follows:

$$\begin{array}{cccc}
\text{Strategic} & & \text{Inc. (dec.)} & \\
\text{substitutability} & \text{Lemma 2} & \text{substitutability} & \text{Lemma 2} \\
< 0 & > 0 & \geq (\leq) 0 & < 0 \\
\overbrace{\frac{\partial^2 \hat{\pi}_i^C}{\partial q_j^* \partial q_i^*}} & \times & \overbrace{\frac{\partial^2 \hat{\pi}_i^C}{\partial (q_j^*)^2}} & \times & \overbrace{\frac{\partial q_j^*}{\partial \beta_j^C} \frac{\partial q_j^*}{\partial \beta_i^C}} \\
\frac{d\beta_i^C}{d\beta_j^C} = - \frac{\frac{\partial^2 \hat{\pi}_i^C}{\partial q_j^* \partial q_i^*} \left(\frac{\partial q_j^*}{\partial \beta_i^C} \right)^2 + \frac{\partial^2 \hat{\pi}_i^C}{\partial q_j^* \partial q_i^*} \frac{\partial q_i^*}{\partial \beta_i^C} \frac{\partial q_j^*}{\partial \beta_i^C} - [(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)]}{\underbrace{\frac{\partial^2 \hat{\pi}_i^C}{\partial (q_j^*)^2} \left(\frac{\partial q_j^*}{\partial \beta_i^C} \right)^2 + \frac{\partial^2 \hat{\pi}_i^C}{\partial q_j^* \partial q_i^*} \frac{\partial q_i^*}{\partial \beta_i^C} \frac{\partial q_j^*}{\partial \beta_i^C} - [(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)]}} & & & (19) \\
< 0 & & &
\end{array}$$

Second-order condition (SOC) of the principal's problem

The intuition underlying the strategic properties of managerial incentives is akin to that we offered in the Bertrand competition case, with one exception. From (16), the quantity equilibrium $\{q_1^*(\beta), q_2^*(\beta)\}$ is linear in the marginal cost of each firm and thereby managerial incentives β . Thus, there is no second effect (i.e., demand supermodularity or submodularity does not play a role), implying only the first and third effects remain.¹⁸ The next proposition summarizes our findings.¹⁹

Proposition 2 (Strategic Incentives with Cournot Competition) *Managerial incentives are strategic substitutes if demand functions exhibit decreasing or weakly increasing substitutability; and they are strategic complements if demand functions exhibit strongly increasing substitutability.*

If demand is linear in the rival's quantity (e.g., $d_i = B - q_i - \nu q_j$), then managerial incentives are strategic substitutes (as are quantities). Overall, then, if demand is linear and

¹⁸By contrast, prices are not linear in marginal costs, so the second effect is present in the Bertrand case.

¹⁹Vives (2009) obtains similar conditions to ours in a model in which, in the first stage, firms make capacity investments that lower marginal cost and, in the second stage, firms compete in Cournot fashion. For a unique equilibrium $\{\beta_1^C, \beta_2^C\}$ of managerial incentives to exist, we require that $\left| \frac{d\beta_i^C}{d\beta_j^C} \right| < 1$. With linear demand, this condition holds for a wide range of parameter values.

additively separable, irrespective of the type of competition, managerial incentives inherit the properties of the strategic variables (prices or quantities) being utilized by firms when competing in the product market.

Similarly, as with Bertrand competition, if firms operate in a perfectly competitive market, then managerial incentives are not strategic.

5 Theoretical Implications of Strategic Managerial Incentives

The manner in which managerial incentives respond to a change in the corporate environment may be decomposed into *direct* and *strategic* effects. The direct effect represents the amount by which a firm's incentives respond to the change in the corporate environment holding fixed its rival's incentives. The strategic effect represents the amount by which a firm's incentives react to the change in its rival's incentives. Therefore, the direct and strategic effects are interrelated, the latter to some degree reflecting the former. A large direct effect for one firm typically translates into a large strategic effect for the other firm.

We first consider a change in the corporate environment that is common to both firms, and then a change in the corporate environment that is specific to one firm. For ease of exposition, we focus on the role of risk, such that the former pertains to systematic risk, while the latter pertains to idiosyncratic risk. However, all the arguments we put forth are applicable across a broad range of changes in the corporate environment, such as those brought about by shifts in managerial practices and corporate governance. For example, when discussing a change in systematic risk, we could alternatively be referring to the passing of Sarbanes-Oxley (in the sense that it affects all firms in the industry); and when discussing a change in the idiosyncratic risk of a firm, we could alternatively be referring to a change in the composition of its board of directors.

5.1 Strategic Managerial Incentives and Systematic Risk

Consider an increase in systematic risk σ^2 . We will show that the direct effect yields the "traditional" response that one would expect from a standard agency model, while the strategic effect operates in the same or opposite direction from the direct effect depending on whether managerial incentives are strategic complements or substitutes, respectively. If managerial incentives are strategic substitutes and the strategic effect is sufficiently strong, then the strategic effect may overpower the direct effect to yield an "unusual" response for one firm and a "traditional" response for another. If managerial incentives are strategic complements, then the strategic effect operates in the same direction as the direct effect, such that both firms experience "traditional" responses; however, the responses are stronger than would be predicted by a standard agency model, leading to a *ratcheting* effect.

5.1.1 Managerial Incentives are Strategic Substitutes

Suppose managerial incentives are strategic substitutes and firms compete in Bertrand fashion.²⁰ Holding constant the managerial incentives of firm j , from (13), we infer that the best-response incentives curve of firm i shifts as follows in response to the increase in systematic risk:²¹

$$\frac{d\beta_i^B}{d\sigma^2} = \frac{\beta_i^B R}{\underbrace{\frac{\partial^2 \pi_i^B}{\partial (p_j^*)^2} \left(\frac{\partial p_j^*}{\partial \beta_i^B} \right)^2 + \frac{\partial^2 \pi_i^B}{\partial p_j^* \partial p_i^*} \frac{\partial p_i^*}{\partial \beta_i^B} \frac{\partial p_j^*}{\partial \beta_i^B} - [(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)]}_{< 0}} < 0. \quad (20)$$

Second-order condition (SOC) of the principal's problem

As expected, greater systematic risk implies lower incentives, all else being equal. But

²⁰See Proposition 1 for the conditions under which this arises. For ease of exposition, we focus on the case in which firms compete in Bertrand fashion. The same arguments apply if firms compete in Cournot fashion.

²¹Note that this expression does not describe the change in equilibrium incentives; rather, it describes the way in which each best-response incentives curve shifts.

in this strategic environment, all else cannot be equal, because the rival responds. Owing to the strategic substitutability of managerial incentives, in equilibrium, it may very well be the case that one firm has strengthened the incentives offered its manager. For this to occur, heterogeneous responses to a change in σ^2 are required (i.e., $d\beta_i^B/d\sigma^2$ is different from $d\beta_j^B/d\sigma^2$).

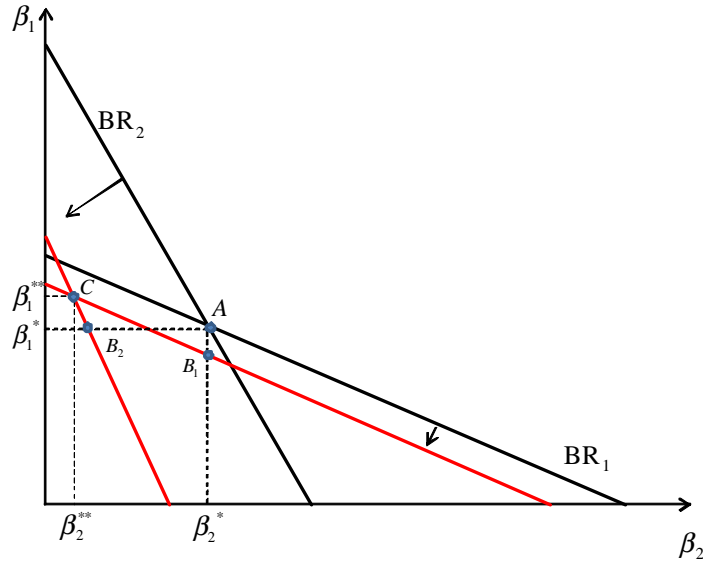


Figure 1: Increase in Systematic Risk when Managerial Incentives are Strategic Substitutes and the Strategic Effect is Strong

Figure 1 illustrates our argument. The curve BR_i represents the best-response function of firm i : it describes the manner in which firm i responds to the managerial incentives being offered by firm j . The initial equilibrium is (β_1^*, β_2^*) . Suppose systematic risk σ^2 increases, leading to the new equilibrium $(\beta_1^{**}, \beta_2^{**})$. Interestingly, firm 1 offers stronger incentives, $\beta_1^{**} > \beta_1^*$, although risk has increased. What is the intuition? An increase in systematic risk leads to a downward shift in both best-response incentives curves. This is the direct effect. However, the best-response incentives curve of firm 2, BR_2 , decreases more than BR_1

because the firms are heterogeneous; by inspecting (20), one notices that the potential source of heterogeneous responses may be differences in idiosyncratic risk σ_i^2 or the sensitivity of marginal cost to managerial effort θ_i , for example. Hence, when systematic risk increases, both firms weaken their incentives, holding the rival's managerial incentives constant. But when the rival offers weaker incentives, the best-response of a firm is to strengthen its incentives since managerial incentives are strategic substitutes. If the strategic effect is strong enough, as it is in Figure 1 for firm 1, then it outweighs the direct effect, the net result of which is a positive relationship between systematic risk and incentives for firm 1 (and a negative relationship between systematic risk and incentives for firm 2).

The direct and strategic effects may be decomposed as follows using Figure 1. The initial equilibrium is point A . The move from point A to point B_1 represents the amount by which the managerial incentives of firm 1 decline due to the downward shift in BR_1 (brought about by the increase in systematic risk) in the absence of a response by firm 2, thus it captures the direct effect associated with firm 1. Similarly, the move from point A to point B_2 is the amount by which the incentives of firm 2 decline due to the downward shift in BR_2 in the absence of a response by firm 1, thus it captures the direct effect of firm 2. The direct effects are negative, in agreement with agency theory which posits that incentives should become weaker in light of greater risk. The new equilibrium is point C . The move from point B_1 to point C represents the amount by which the incentives of firm 1 strengthen due to the response by firm 2 to the increase in systematic risk, capturing the strategic effect of firm 1. Because firm 2 weakens its incentives significantly as a consequence of the increase in systematic risk (i.e., the downward shift in BR_2 is large), firm 1 responds by strengthening its incentives considerably since incentives are strategic substitutes. In this example, the strategic effect is strong enough to overpower the direct effect, such that firm 1 experiences a net increase in its incentives (from β_1^* to β_1^{**}). The move from point B_2 to point C represents the amount by which the incentives of firm 2 weaken due to the response by firm 1 to the increase in systematic risk, capturing the strategic effect of firm 2.

To identify which firm may strengthen its managerial incentives in response to an increase in systematic risk, consider the following. In Figure 1, firm 2 has a large response (direct effect) to the increase in risk, which leads firm 1 to have a strong strategic effect; and firm 1 has a small response (direct effect) to the increase in systematic risk, which leads firm 2 to have a weak strategic effect. The net effects are that firm 1 strengthens its incentives while firm 2 weakens them. Therefore, the firm that is less sensitive to systematic risk (i.e., the one with the small direct effect) is the one for which we obtain an unusual response.

In Raith (2003), piece rates are positively correlated with the variance of firm profit across markets that differ in product substitutability, market size, or entry costs. Therefore, in Raith, a positive link between risk and incentives arises across heterogeneous industries. By contrast, we may obtain positive and negative links across heterogeneous firms in the same industry.

If managerial incentives are strategic substitutes, but the strategic effect does not overpower the direct effect, then the strategic effect serves to *dampen* the response of managerial incentives to a change in the corporate environment common to all firms in the industry. Figure 2 illustrates an increase in systematic risk, which moves the equilibrium from point A to point C . The moves from point A to points B_1 and B_2 represent the (negative) direct effects of firms 1 and 2. The moves from points B_1 and B_2 to point C represent the (positive) strategic effects. For each firm, because its rival weakens its incentives, the strategic response is to strengthen incentives (since incentives are strategic substitutes). However, in neither case is the strategic effect strong enough to overpower the direct effect. Thus, the strategic effect dampens the extent to which the incentives of each firm decline as a consequence of the increase in systematic risk. This scenario arises if firms are homogeneous, or they are

not extensively heterogeneous.

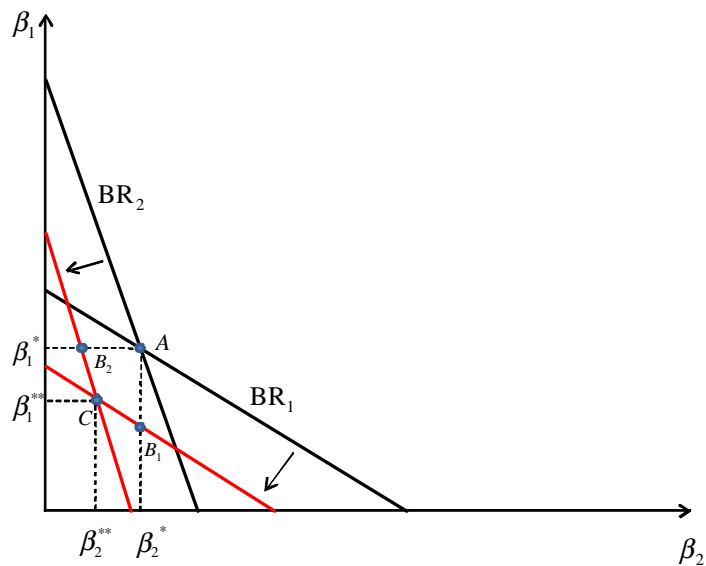


Figure 2: Increase in Systematic Risk when Managerial Incentives are Strategic Substitutes and the Strategic Effect is Weak

5.1.2 Managerial Incentives are Strategic Complements

Suppose managerial incentives are strategic complements. Then the strategic effect operates in the same direction as the direct effect. Thus, strategic considerations serve to *amplify* the response of managerial incentives to a change in the corporate environment common to both firms. Consider an increase in systematic risk σ^2 , as illustrated in Figure 3. The moves from point A to points B_1 and B_2 representing the direct effects of firms 1 and 2 are relatively weak. In the absence of strategic considerations, neither firm would respond significantly to the increase in systematic risk. However, when we take into account the strategic effects represented by the moves from points B_1 and B_2 to point C , we see that the net changes in incentives are considerable. Extrapolating these findings into industries characterized by multiple firms competing against each other, we infer that a drastic *ratcheting* effect may

occur. That is, seemingly small changes in the corporate environment common to all firms in the industry can lead to dramatic changes in managerial incentives. As each firm in the industry reacts strategically to each other firm, the overall response is magnified as it permeates the entire industry.

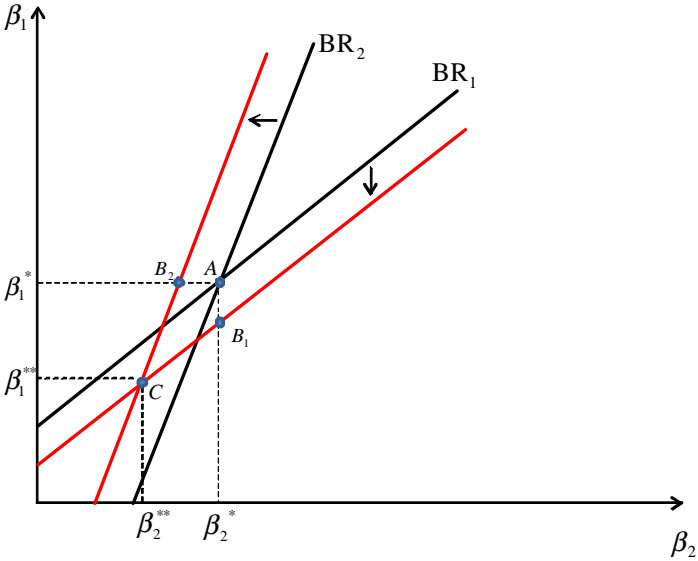


Figure 3: Increase in Systematic Risk when Managerial Incentives are Strategic Complements

5.2 Managerial Incentives and Idiosyncratic Risk

When there is a change in the idiosyncratic risk of a firm, the best-response incentives curve of that firm shifts, while the other firm experiences a movement along its best-response incentives curve. Thus, in light of strategic considerations, all firms in the industry respond to changes in a firm’s idiosyncratic risk. To illustrate this, suppose managerial incentives are strategic complements and consider an increase in the idiosyncratic risk σ_1^2 faced by firm 1. This shifts downward the best-response incentives curve of firm 1, and represents a movement along the best-response incentives curve of firm 2. Firm 1 weakens its incentives

due to risk-sharing considerations, and firm 2 responds by weakening its incentives since managerial incentives are strategic complements, as shown in Figure 4. In a traditional agency model, there would be no change in the incentives offered by firm 2 (that is, there is no strategic effect). In broad terms, this means that when a firm experiences a change in its specific corporate environment that leads it to adapt its compensation scheme, all the firm’s competitors react by adapting their compensation schemes; if managerial incentives are strategic complements (substitutes), then their reactions move in the same (opposite, respectively) direction.

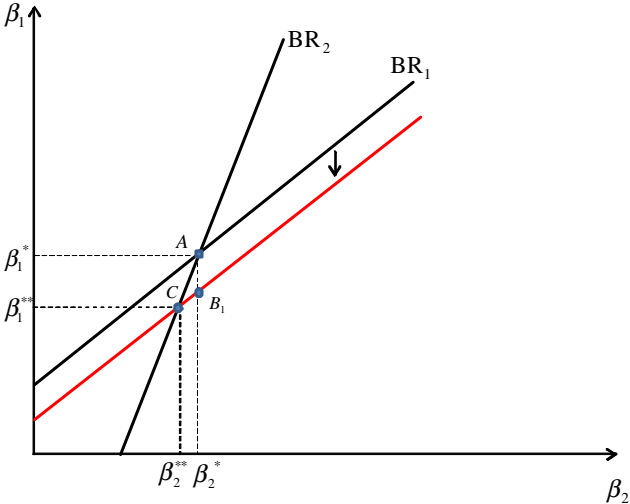


Figure 4: Increase in the Idiosyncratic Risk of Firm 1 when Managerial Incentives are Strategic Complements

6 Empirical Implications of Strategic Managerial Incentives

Our model suggests numerous avenues for future empirical research. First, the strategic nature of managerial compensation schemes is itself empirically testable. That is, we should

find that a change in the compensation scheme offered by a firm should cause its rivals to respond by changing their compensation schemes. These predictions are testable in terms of both compensation levels and incentives. Because firms typically engage in various forms of competition utilizing a wide variety of strategic tools spanning a number of products and industries, observed changes in compensation schemes reflect the agglomeration of all these (direct and strategic) effects. Indeed, Kedia (2006) finds that 29 percent of 4-digit SIC industries use both strategic complements and substitutes when competing. Hence, we postulate that the most practical approach is to test directly the strategic relationship of compensation levels and incentives, rather than attempt to infer them from the characteristics of the product markets in which the firms are competing. If the compensation schemes of a collection of firms are not found to be strategic, then the model predicts that those firms are engaged in perfect competition, or the strategic effects we identified are weak. Kedia finds that 29 percent of 4-digit SIC industries are not engaged in strategic interaction, suggesting they are perfectly competitive.

Second, the strategic property of compensation levels has ramifications in terms of the setting and formulation of benchmark pay (Bizjak, Lemmon, and Naveen 2008; Faulkender and Yang 2010). In evaluating the importance of benchmarking, the empirical literature has appealed to the agency theoretic prediction that, at the optimum, an agent should be offered his reservation utility (in a standard model with moral hazard). Our analysis suggests there is also a strategic motive stemming from the product market. In a random sample of 100 S&P 500 firms, Bizjak, Lemmon, and Naveen study proxy statements to find that peer groups are typically based on industry and size, suggesting they may be competitors; and that the majority of firms using benchmarking target their pay levels at or above the median of their peer group. The key point we make is that benchmarking (via formal and informal means) may be implemented not only to ensure the CEO remains with the firm by setting reservation wages, but also as a consequence of the fact that the firms are competing strategically in the marketplace.

Third, the model predicts that if compensation schemes are strategic complements, then a ratcheting effect of CEO compensation levels and incentives occurs. Specifically, consider a change in the corporate environment common to all firms in the industry that leads them to increase their compensation levels and incentives (the "direct" effect). Due to strategic complementarity, each firm responds to the other by further increasing its compensation (the "strategic" effect). It is thereby possible that strategic considerations contributed towards the dramatic rise in U.S. CEO pay, which increased sixfold between 1980 and 2003, as well as the sharp rise in pay-performance sensitivity during the mid-1980s to 2005 (Gabaix and Landier 2008; Frydman and Saks 2010).

Fourth, in examining the empirical link between managerial compensation schemes and changes in the corporate environment, we propose that such changes be decomposed into components that are firm-specific versus common to all firms whenever possible. For example, firm risk should be decomposed into idiosyncratic and systematic risk. The model predicts that managerial incentives respond to a change in a firm's specific corporate environment (e.g., idiosyncratic risk) in the usual fashion consistent with agency theory, whereas managerial incentives may respond to a change in the corporate environment common to all firms in the industry (e.g., systematic risk) in a fashion that dispels traditional agency theory.

Fifth, future empirical work should test the prediction that a change in the corporate environment specific to a firm may cause not just the firm itself to adjust its compensation scheme, but also cause the firm's rivals to adjust their compensation schemes due to the strategic effects we identified. We showed that while an increase in the idiosyncratic risk of a firm leads it to weaken its managerial incentives (in accord with traditional agency theory), the rival responds by strengthening (weakening) its incentives if compensation schemes are strategic substitutes (complements, respectively). In this sense, idiosyncratic risk may become endowed with characteristics previously solely attributed to systematic risk. Another example would be a change in a firm's board of directors that leads the firm to change

the compensation scheme of its CEO. The firm's competitors may react by adapting their compensation schemes even though they were not directly affected by the change in the firm's board; such reactions would not relate to the retention concern, but instead the fact that managers may have to be incentivized more or less aggressively to be successful in the product market.

Sixth, the relationship between managerial compensation schemes and the corporate environment common to all firms in the industry may be asymmetric across firms, suggesting that a broad set of moderating factors should be considered in empirical studies of executive compensation. For example, the model predicts that, if firms are heterogeneous and managerial incentives are strategic substitutes, then an increase in systematic risk may strengthen the incentives offered by one set of firms and weaken the incentives offered by another set. It is important to emphasize that this holds true across firms in the same industry, and not just across industries. This may explain why some empirical studies find that the relationship between risk and incentives is positive (Core and Guay 1999; Oyer and Schaefer 2005; Rajgopal, Shevlin, and Zamora 2006); some find that the link is insignificant (Garen 1994; Yermack 1995; Bushman, Indjejikian, and Smith 1996; Ittner, Larcker, and Rajan 1997; Conyon and Murphy 2000); and others find that the link is negative (Lambert and Larcker 1987; Aggarwal and Samwick 1999a; Jin 2002). Because there are numerous sources of heterogeneity across firms (both within and across industries), empirical researchers will have to determine which firm characteristics significantly moderate the relationship between managerial incentives and firm risk. One such moderating factor may be firm size. In general, any event that affects all firms in the industry (such as a regulatory change, e.g. Sarbanes-Oxley) may lead firms to adapt their compensation schemes in opposite directions, not because firms are fundamentally heterogeneous (which in and of itself is not sufficient to generate asymmetry), but because of the strategic effects we uncovered.

Finally, there is considerable evidence that an increase in the extent of competition is associated with a strengthening of managerial incentives (DeFond and Park 1999; Hubbard

and Palia 1995; Cunat and Guadalupe 2005, 2009; Karuna 2007).²² A number of theoretical papers use different models to examine the link between product market competition and pay-performance sensitivity, and predict either an ambiguous or positive relationship (Raith 2003; Schmidt 1997; Hart 1983; Scharfstein 1988; Hermalin 1992). The strategic considerations we identified may shed light on this debate. Karuna (2007) examines three industry characteristics emphasized by Raith (2003) that determine the extent to which an industry is competitive: the cost of entry, market size, and the degree of product differentiation. A related study is due to Krishnan (2005), who finds that, among California hospitals, there is no association between the intensity of competition and the demand for accounting information when firms engage in quality competition; but when firms compete in prices, the need to control costs leads to a positive association between the two. A recurring theme of our model is that, due to firm heterogeneity and strategic behavior, changes in the corporate environment may lead to asymmetric responses in managerial compensation across firms in the same industry. Therefore, future empirical work should consider allowing for this possibility by examining firm-specific moderating factors in testing the relationship between the extent of competition and compensation.

7 Conclusion

This paper demonstrated that managerial compensation schemes are strategic due to product market competition. We derived reasonable conditions under which managerial compensation levels and incentives are strategic substitutes or complements. These conditions relate to the form of competition (Bertrand or Cournot), the characteristics of the demand for the product, and the properties of the strategic variables being wielded by firms when competing in the product market. If firms operate in a perfectly competitive market, then compensation schemes are not strategic. We demonstrated that the strategic nature of

²²A related study is due to Joh (1999), who finds that, in Japan, managerial compensation is positively linked to industry profit, the positive effect being stronger in competitive industries than in concentrated industries.

managerial compensation schemes has implications for the ways in which firms adapt their compensation in response to changes in their own corporate environment, the environments of their rivals, and the environment common to all firms operating in the industry. The ramifications of strategic compensation schemes are numerous. We emphasized the following: the conventional wisdom may no longer hold about the precision of the performance measure and managerial incentives; the corporate environment specific to one firm influences the design of compensation schemes across all firms in the industry; and a ratcheting effect of compensation may occur that amplifies otherwise small changes in the corporate environment common to all firms in the industry.

Our findings suggest the following avenues for future theoretical research. First, our predictions about the strategic nature of managerial compensation schemes should naturally extend to an environment with more than two firms. The strategic relationship between the compensation schemes of any pair of firms is a function of how the demands for their products are inter-related and whether the strategic variables utilized by the firms in the product market are strategic substitutes or complements.

Second, one may expand the set of strategic tools being wielded by firms when competing in the product market. We focused on the traditional forms of competition emphasized in economics, namely price and quantity competition. However, our basic arguments should also be applicable under other, perhaps more exotic, forms of competition. For example, the realm of competition may include capital expenditures; R&D expenses to improve the quality of the product and lower costs of production; and advertising expenses to increase demand. One would then have to determine whether such strategic variables are strategic complements or substitutes, and the extent to which the strategy of one firm affects the demand of another.

Third, along the lines of Bolton and Scharfstein (1990), Rotemberg and Scharfstein (1990), and Maksimovic (1988), future theoretical work should aim to uncover the strategic properties of capital structures that arise from product market competition. Just as firms

react to one another's compensation schemes, one may find that firms react to one another's capital structures. The literature shows that debt serves as a commitment device that disciplines management towards behaving with a more aggressive or defensive posture depending on the characteristics of the product market. Thus, we postulate that, under certain conditions, firms make capital structure decisions to incentivize their managers to respond to and be more successful against their competitors in the product market.

A Appendix: Proofs of Lemmas and Propositions

A.1 Proof of Lemma 1

We invoke the Implicit Function Theorem using the system of first order conditions given by (8) :

$$\begin{aligned}
 \begin{pmatrix} \frac{\partial p_1^*}{\partial \beta_1} & \frac{\partial p_1^*}{\partial \beta_2} \\ \frac{\partial p_2^*}{\partial \beta_1} & \frac{\partial p_2^*}{\partial \beta_2} \end{pmatrix} &= - \begin{pmatrix} \frac{\partial^2 \pi_1}{\partial p_1^2} & \frac{\partial^2 \pi_1}{\partial p_1 \partial p_2} \\ \frac{\partial^2 \pi_2}{\partial p_2 \partial p_1} & \frac{\partial^2 \pi_2}{\partial p_2^2} \end{pmatrix}^{-1} \begin{pmatrix} \frac{\partial D_1}{\partial p_1} (\theta_1 + \theta)^2 & 0 \\ 0 & \frac{\partial D_2}{\partial p_2} (\theta_2 + \theta)^2 \end{pmatrix} \\
 &= -\frac{1}{\Delta} \begin{pmatrix} \frac{\partial^2 \pi_2}{\partial p_2^2} & -\frac{\partial^2 \pi_1}{\partial p_1 \partial p_2} \\ -\frac{\partial^2 \pi_2}{\partial p_2 \partial p_1} & \frac{\partial^2 \pi_1}{\partial p_1^2} \end{pmatrix} \begin{pmatrix} \frac{\partial D_1}{\partial p_1} (\theta_1 + \theta)^2 & 0 \\ 0 & \frac{\partial D_2}{\partial p_2} (\theta_2 + \theta)^2 \end{pmatrix} \\
 &= -\frac{1}{\Delta} \begin{pmatrix} \frac{\partial^2 \pi_2}{\partial p_2^2} \frac{\partial D_1}{\partial p_1} (\theta_1 + \theta)^2 & -\frac{\partial^2 \pi_1}{\partial p_1 \partial p_2} \frac{\partial D_2}{\partial p_2} (\theta_2 + \theta)^2 \\ -\frac{\partial^2 \pi_2}{\partial p_2 \partial p_1} \frac{\partial D_1}{\partial p_1} (\theta_1 + \theta)^2 & \frac{\partial^2 \pi_1}{\partial p_1^2} \frac{\partial D_2}{\partial p_2} (\theta_2 + \theta)^2 \end{pmatrix},
 \end{aligned}$$

where $\Delta \equiv \frac{\partial^2 \pi_1}{\partial p_1^2} \frac{\partial^2 \pi_2}{\partial p_2^2} - \frac{\partial^2 \pi_1}{\partial p_1 \partial p_2} \frac{\partial^2 \pi_2}{\partial p_2 \partial p_1}$ is the determinant of the Jacobian of the system of first-order conditions. From Assumption 2, Δ is strictly positive. It then follows that

$$\frac{\partial p_i^*}{\partial \beta_i} = -\frac{1}{\Delta} \left(\frac{\partial^2 \pi_j}{\partial p_j^2} \frac{\partial D_i}{\partial p_i} (\theta_i + \theta)^2 \right) \quad (21)$$

$$= -\frac{1}{\Delta} \left((p_j - (c - \beta_j(\theta_j + \theta)^2)) \frac{\partial^2 D_j}{\partial p_j^2} + 2 \frac{\partial D_j}{\partial p_j} \right) \frac{\partial D_i}{\partial p_i} (\theta_i + \theta)^2 < 0;$$

$$\begin{aligned}
 \frac{\partial p_i^*}{\partial \beta_j} &= \frac{1}{\Delta} \left(\frac{\partial^2 \pi_i}{\partial p_i \partial p_j} \frac{\partial D_j}{\partial p_j} (\theta_j + \theta)^2 \right) \\
 &= \frac{1}{\Delta} \left((p_i - (c - \beta_i(\theta_i + \theta)^2)) \frac{\partial^2 D_i}{\partial p_j \partial p_i} + \frac{\partial D_i}{\partial p_i} \right) \frac{\partial D_j}{\partial p_j} (\theta_j + \theta)^2 < 0. \quad (22)
 \end{aligned}$$

The above signs follow from Assumption 1 and the facts that prices are strategic complements and demand is downward sloping in its own price. Also note that the strength of $|\partial p_i^* / \partial \beta_j|$ depends positively on how strong the strategic complementarity $\partial^2 \pi_i / (\partial p_i \partial p_j)$ is. The strength of the strategic complementarity in turn depends on β_i . If demand is super-modular, $\partial^2 D_i / (\partial p_j \partial p_i) > 0$, then the higher the β_i the higher the $|\partial p_i^* / \partial \beta_j|$. The opposite

holds when demand is submodular, $\partial^2 D_i / (\partial p_j \partial p_i) < 0$.

For use in the proof of Proposition 1, note, using (22), that $\partial p_i^* / \partial \beta_j$ does not depend on β_j , i.e., $\partial^2 p_i / \partial \beta_j^2 = 0$ and $\partial^2 p_j / \partial \beta_i^2 = 0$. However, $\partial p_i^* / \partial \beta_j$ does depend on β_i , as we have argued above.

A.2 Proof of Proposition 1

We would like to determine how β_j affects β_i (the slope of principal i 's reaction function with respect to incentives). We will totally differentiate the first order condition (13). The first term in (13) is zero from the envelope theorem, the second term is the strategic effect, the third term captures the direct effect of incentives on production cost and the last term is the cost associated with incentivizing the agent. The strategic term $\frac{\partial \pi_i^B}{\partial p_j^*} \frac{\partial p_j^*}{\partial \beta_i^B}$ depends on $\beta = (\beta_1, \beta_2)$ as follows: first, β affects the equilibrium prices (p_1^*, p_2^*) and thus the profit function π_i^B , which suggests that it affects the term $\partial \pi_i^B / \partial p_j^*$ and second, β affects the way equilibrium prices react to changes in incentives, i.e., the term $\partial p_j^* / \partial \beta_i^B$. Therefore, differentiating the strategic effect with respect to either β_i or β_j will yield three terms. Furthermore, the third term in (13), since cost reduction depends only on β_i linearly, is independent of β .

Thus, by totally differentiating (13) with respect to β_i and β_j we obtain:

$$\left\{ \frac{\partial^2 \pi_i}{\partial p_j^2} \left(\frac{\partial p_j}{\partial \beta_i} \right)^2 + \frac{\partial^2 \pi_i}{\partial p_j \partial p_i} \frac{\partial p_i}{\partial \beta_i} \frac{\partial p_j}{\partial \beta_i} + \frac{\partial \pi_i}{\partial p_j} \frac{\partial^2 p_j}{\partial \beta_i^2} - [(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)] \right\} d\beta_i + \left\{ \frac{\partial^2 \pi_i}{\partial p_j^2} \frac{\partial p_j}{\partial \beta_j} \frac{\partial p_j}{\partial \beta_i} + \frac{\partial^2 \pi_i}{\partial p_j \partial p_i} \frac{\partial p_i}{\partial \beta_j} \frac{\partial p_j}{\partial \beta_i} + \frac{\partial \pi_i}{\partial p_j} \frac{\partial^2 p_j}{\partial \beta_i \partial \beta_j} \right\} d\beta_j = 0.$$

From Lemma 1 we know that $\partial^2 p_j / \partial \beta_i^2 = 0$. Then, the above expression reduces to

$$\begin{aligned}
& \left\{ \frac{\partial^2 \pi_i}{\partial p_j^2} \left(\frac{\partial p_j}{\partial \beta_i} \right)^2 + \frac{\partial^2 \pi_i}{\partial p_j \partial p_i} \frac{\partial p_i}{\partial \beta_i} \frac{\partial p_j}{\partial \beta_i} - [(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)] \right\} d\beta_i + \\
& \left\{ \frac{\partial^2 \pi_i}{\partial p_j^2} \frac{\partial p_j}{\partial \beta_j} \frac{\partial p_j}{\partial \beta_i} + \frac{\partial^2 \pi_i}{\partial p_j \partial p_i} \frac{\partial p_i}{\partial \beta_j} \frac{\partial p_j}{\partial \beta_i} \frac{\partial p_i}{\partial p_j} + \frac{\partial \pi_i}{\partial p_j} \frac{\partial^2 p_j}{\partial \beta_i \partial \beta_j} \right\} d\beta_j = 0 \Leftrightarrow \\
& \frac{d\beta_i}{d\beta_j} = - \frac{\frac{\partial^2 \pi_i}{\partial p_j^2} \frac{\partial p_j}{\partial \beta_j} \frac{\partial p_j}{\partial \beta_i} + \frac{\partial^2 \pi_i}{\partial p_j \partial p_i} \frac{\partial p_i}{\partial \beta_j} \frac{\partial p_j}{\partial \beta_i} + \frac{\partial \pi_i}{\partial p_j} \frac{\partial^2 p_j}{\partial \beta_i \partial \beta_j}}{\frac{\partial^2 \pi_i}{\partial p_j^2} \left(\frac{\partial p_j}{\partial \beta_i} \right)^2 + \frac{\partial^2 \pi_i}{\partial p_j \partial p_i} \frac{\partial p_i}{\partial \beta_i} \frac{\partial p_j}{\partial \beta_i} - [(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)]}.
\end{aligned}$$

If $|d\beta_i/d\beta_j| < 1$ we obtain a unique equilibrium (β_1^*, β_2^*) . The denominator of $d\beta_i/d\beta_j$ is the second derivative of the profit function with respect to β_i , which is negative due to the SOC of the principal's problem. The sign of the numerator is ambiguous and we discuss the three effects (stemming from the three different terms in the numerator) in the main text.

A.3 Proof of Lemma 2

We invoke the Implicit Function Theorem using the system of first-order conditions given by (16):

$$\begin{aligned}
\begin{pmatrix} \frac{\partial q_1^*}{\partial \beta_1} & \frac{\partial q_1^*}{\partial \beta_2} \\ \frac{\partial q_2^*}{\partial \beta_1} & \frac{\partial q_2^*}{\partial \beta_2} \end{pmatrix} &= - \begin{pmatrix} \frac{\partial^2 \hat{\pi}_1}{\partial q_1^2} & \frac{\partial^2 \hat{\pi}_1}{\partial q_1 \partial q_2} \\ \frac{\partial^2 \hat{\pi}_2}{\partial q_2 \partial q_1} & \frac{\partial^2 \hat{\pi}_2}{\partial q_2^2} \end{pmatrix}^{-1} \begin{pmatrix} (\theta_1 + \theta)^2 & 0 \\ 0 & (\theta_2 + \theta)^2 \end{pmatrix} \\
&= -\frac{1}{\Delta} \begin{pmatrix} \frac{\partial^2 \hat{\pi}_2}{\partial q_2^2} & -\frac{\partial^2 \hat{\pi}_1}{\partial q_1 \partial q_2} \\ -\frac{\partial^2 \hat{\pi}_2}{\partial q_2 \partial q_1} & \frac{\partial^2 \hat{\pi}_1}{\partial q_1^2} \end{pmatrix} \begin{pmatrix} (\theta_1 + \theta)^2 & 0 \\ 0 & (\theta_2 + \theta)^2 \end{pmatrix} \\
&= -\frac{1}{\Delta} \begin{pmatrix} \frac{\partial^2 \hat{\pi}_2}{\partial q_2^2} (\theta_1 + \theta)^2 & -\frac{\partial^2 \hat{\pi}_1}{\partial q_1 \partial q_2} (\theta_2 + \theta)^2 \\ -\frac{\partial^2 \hat{\pi}_2}{\partial q_2 \partial q_1} (\theta_1 + \theta)^2 & \frac{\partial^2 \hat{\pi}_1}{\partial q_1^2} (\theta_2 + \theta)^2 \end{pmatrix},
\end{aligned}$$

where $\Delta \equiv \frac{\partial^2 \hat{\pi}_1}{\partial q_1^2} \frac{\partial^2 \hat{\pi}_2}{\partial q_2^2} - \frac{\partial^2 \hat{\pi}_1}{\partial q_1 \partial q_2} \frac{\partial^2 \hat{\pi}_2}{\partial q_2 \partial q_1}$ is the determinant of the Jacobian of the system of first-order conditions. From Assumption 2, Δ is strictly positive. It then follows that

$$\frac{\partial q_i^*}{\partial \beta_i} = -\frac{1}{\Delta} \left(\frac{\partial^2 \hat{\pi}_j}{\partial q_j^2} (\theta_i + \theta)^2 \right) = -\frac{1}{\Delta} \left(\frac{\partial^2 d_j}{\partial q_j^2} q_j + 2 \frac{\partial d_j}{\partial q_j} \right) (\theta_i + \theta)^2 > 0; \quad (23)$$

$$\frac{\partial q_i^*}{\partial \beta_j} = \frac{1}{\Delta} \left(\frac{\partial^2 \hat{\pi}_i}{\partial q_i \partial q_j} (\theta_j + \theta)^2 \right) = \frac{1}{\Delta} \left(\frac{\partial^2 d_i}{\partial q_i \partial q_j} q_i + \frac{\partial d_i}{\partial q_j} \right) (\theta_j + \theta)^2 < 0. \quad (24)$$

The above signs follow from Assumption 1 and the fact that quantities are strategic substitutes. Note that the above derivatives do not depend on β .

A.4 Proof of Proposition 2

Following a similar logic as in the proof of Proposition 1, we totally differentiate (18) with respect to β_i and β_j in order to determine the slope of the reaction functions:

$$\left\{ \frac{\partial^2 \hat{\pi}_i}{\partial q_j^2} \left(\frac{\partial q_j}{\partial \beta_i} \right)^2 + \frac{\partial^2 \hat{\pi}_i}{\partial q_j \partial q_i} \frac{\partial q_i}{\partial \beta_i} \frac{\partial q_j}{\partial \beta_i} + \frac{\partial \hat{\pi}_i}{\partial \beta_i} \frac{\partial^2 q_j}{\partial \beta_i^2} - [(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)] + \frac{\partial^2 \hat{\pi}_i}{\partial \beta_i^2} \right\} d\beta_i +$$

$$\left\{ \frac{\partial^2 \hat{\pi}_i}{\partial q_j^2} \frac{\partial q_j}{\partial \beta_j} \frac{\partial q_j}{\partial \beta_i} + \frac{\partial^2 \hat{\pi}_i}{\partial q_j \partial q_i} \frac{\partial q_i}{\partial \beta_j} \frac{\partial q_j}{\partial \beta_i} + \frac{\partial \hat{\pi}_i}{\partial q_j} \frac{\partial^2 q_j}{\partial \beta_i \partial \beta_j} + \frac{\partial^2 \hat{\pi}_i}{\partial \beta_i \partial \beta_j} \right\} d\beta_j = 0.$$

From (24), $\partial^2 q_j / \partial \beta_i^2$ and $\partial^2 q_j / (\partial \beta_i \partial \beta_j)$ are also zero (incentives do not affect the slope of q_i^* with respect to β_i or β_j). Then, the above expression becomes

$$\left\{ \frac{\partial^2 \hat{\pi}_i}{\partial q_j^2} \left(\frac{\partial q_j}{\partial \beta_i} \right)^2 + \frac{\partial^2 \hat{\pi}_i}{\partial q_j \partial q_i} \frac{\partial q_i}{\partial \beta_i} \frac{\partial q_j}{\partial \beta_i} - [(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)] \right\} d\beta_i +$$

$$\left\{ \frac{\partial^2 \hat{\pi}_i}{\partial q_j^2} \frac{\partial q_j}{\partial \beta_j} \frac{\partial q_j}{\partial \beta_i} + \frac{\partial^2 \hat{\pi}_i}{\partial q_j \partial q_i} \frac{\partial q_i}{\partial \beta_j} \frac{\partial q_j}{\partial \beta_i} \right\} d\beta_j = 0 \Leftrightarrow$$

$$\frac{d\beta_i}{d\beta_j} = - \frac{\frac{\partial^2 \hat{\pi}_i}{\partial q_j^2} \frac{\partial q_j}{\partial \beta_j} \frac{\partial q_j}{\partial \beta_i} + \frac{\partial^2 \hat{\pi}_i}{\partial q_j \partial q_i} \frac{\partial q_i}{\partial \beta_j} \frac{\partial q_j}{\partial \beta_i}}{\frac{\partial^2 \hat{\pi}_i}{\partial q_j^2} \left(\frac{\partial q_j}{\partial \beta_i} \right)^2 + \frac{\partial^2 \hat{\pi}_i}{\partial q_j \partial q_i} \frac{\partial q_i}{\partial \beta_i} \frac{\partial q_j}{\partial \beta_i} - [(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)]}.$$

The denominator of $d\beta_i/d\beta_j$ is the second derivative of the profit function with respect to

β_i , which is negative due to the SOC of the principal's problem. The sign of the numerator is ambiguous and we discuss the two effects (stemming from the two different terms in the numerator) in the main text.

B Appendix: Strategic Managerial Compensation Levels

We show that the expected total compensation levels of managers exhibit the same strategic properties as managerial incentives. To achieve this, we transform the firm's problem into one in which compensation levels instead of incentives are being chosen. To begin with, apply the binding individual rationality (IR) constraint, $E(t_i) = r + (\beta_i)^2[(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)]/2$, to obtain an expression for the manager's incentives as a function of his expected total compensation:

$$\beta_i = \left(\frac{2(E(t_i) - r)}{(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)} \right)^{1/2}. \quad (25)$$

The firm's expected marginal cost becomes

$$E(c_i) = c - \left(\frac{2(E(t_i) - r)}{(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)} \right)^{1/2} (\theta_i + \theta)^2. \quad (26)$$

The greater is the manager's expected total compensation, the smaller is the firm's marginal cost of production.

We consider Bertrand competition. The case with Cournot competition is similar, so it is omitted. For the sake of brevity, we do not state the equivalent assumptions that are required, which can be inferred from the corresponding cases with managerial incentives.

As before, firm i 's expected gross profit is given by $\pi_i(p) = (p_i - (c - \beta_i(\theta_i + \theta)^2)) D_i(p)$. Applying equation (26), it becomes

$$\pi_i(p) = \left(p_i - \left(c - \left(\frac{2(E(t_i) - r)}{(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)} \right)^{1/2} (\theta_i + \theta)^2 \right) \right) D_i(p). \quad (27)$$

The FOC with respect to the firm's price is

$$\frac{\partial \pi_i}{\partial p_i} = \left(p_i - \left(c - \left(\frac{2(E(t_i) - r)}{(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)} \right)^{1/2} (\theta_i + \theta)^2 \right) \right) \frac{\partial D_i}{\partial p_i} + D_i(p) = 0. \quad (28)$$

The following lemma derives the manner in which compensation levels affect equilibrium prices:

Lemma 3 (Compensation and Prices with Bertrand Competition) *The equilibrium price of firm i is decreasing in the expected total compensation of its manager, i.e. $\partial p_i^*/\partial E(t_i) < 0$, and decreasing in the expected total compensation of its rival's manager, since prices are strategic complements, i.e. $\partial p_i^*/\partial E(t_j) < 0$.*

Proof. Define the matrix

$$M \equiv \begin{pmatrix} \left(\frac{2(E(t_1) - r)}{(\theta_1 + \theta)^2 + R(\sigma_1^2 + \sigma^2)} \right)^{-1/2} \frac{\partial D_1}{\partial p_1} (\theta_1 + \theta)^2 & 0 \\ 0 & \left(\frac{2(E(t_2) - r)}{(\theta_2 + \theta)^2 + R(\sigma_2^2 + \sigma^2)} \right)^{-1/2} \frac{\partial D_2}{\partial p_2} (\theta_2 + \theta)^2 \end{pmatrix}.$$

We invoke the Implicit Function Theorem:

$$\begin{aligned} \begin{pmatrix} \frac{\partial p_1^*}{\partial E(t_1)} & \frac{\partial p_1^*}{\partial E(t_2)} \\ \frac{\partial p_2^*}{\partial E(t_1)} & \frac{\partial p_2^*}{\partial E(t_2)} \end{pmatrix} &= - \begin{pmatrix} \frac{\partial^2 \pi_1}{\partial p_1^2} & \frac{\partial^2 \pi_1}{\partial p_1 \partial p_2} \\ \frac{\partial^2 \pi_2}{\partial p_2 \partial p_1} & \frac{\partial^2 \pi_2}{\partial p_2^2} \end{pmatrix}^{-1} M = -\frac{1}{\Delta} \begin{pmatrix} \frac{\partial^2 \pi_2}{\partial p_2^2} & -\frac{\partial^2 \pi_1}{\partial p_1 \partial p_2} \\ -\frac{\partial^2 \pi_2}{\partial p_2 \partial p_1} & \frac{\partial^2 \pi_1}{\partial p_1^2} \end{pmatrix} M \\ &= -\frac{1}{\Delta} \begin{pmatrix} \frac{\partial^2 \pi_2}{\partial p_2^2} \left(\frac{2(E(t_1) - r)}{(\theta_1 + \theta)^2 + R(\sigma_1^2 + \sigma^2)} \right)^{-1/2} \frac{\partial D_1}{\partial p_1} (\theta_1 + \theta)^2 & -\frac{\partial^2 \pi_1}{\partial p_2 \partial p_1} \left(\frac{2(E(t_2) - r)}{(\theta_2 + \theta)^2 + R(\sigma_2^2 + \sigma^2)} \right)^{-1/2} \frac{\partial D_2}{\partial p_2} (\theta_2 + \theta)^2 \\ -\frac{\partial^2 \pi_2}{\partial p_1 \partial p_2} \left(\frac{2(E(t_1) - r)}{(\theta_1 + \theta)^2 + R(\sigma_1^2 + \sigma^2)} \right)^{-1/2} \frac{\partial D_1}{\partial p_1} (\theta_1 + \theta)^2 & \frac{\partial^2 \pi_1}{\partial p_1^2} \left(\frac{2(E(t_2) - r)}{(\theta_2 + \theta)^2 + R(\sigma_2^2 + \sigma^2)} \right)^{-1/2} \frac{\partial D_2}{\partial p_2} (\theta_2 + \theta)^2 \end{pmatrix}, \end{aligned}$$

where $\Delta \equiv \frac{\partial^2 \pi_1}{\partial p_1^2} \frac{\partial^2 \pi_2}{\partial p_2^2} - \frac{\partial^2 \pi_1}{\partial p_1 \partial p_2} \frac{\partial^2 \pi_2}{\partial p_2 \partial p_1}$ is the determinant of the Jacobian of the system of first-order conditions. The remainder follows as in the case with managerial incentives. ■

The intuition is the same as in the case with managerial incentives. If firm i enhances the compensation of its manager, this lowers the firm's expected marginal cost and thereby price due to greater managerial effort, i.e. $\partial p_i^*/\partial E(t_i) < 0$. Given the strategic complementarity of prices, the rival responds by lowering its price, $\partial p_j^*/\partial E(t_i) < 0$.

We now derive the equilibrium set of expected total compensation levels. The principal's objective is

$$\begin{aligned}\pi_i^B - E(t_i^B) &= \left(p_i^*(E(t^B)) - \left(c - \left(\frac{2(E(t_i^B) - r)}{(\theta_i + \theta)^2 + R(\sigma_i^2 + \sigma^2)} \right)^{1/2} (\theta_i + \theta)^2 \right) \right) D_i(p^*(E(t^B))) - E(t_i^B) \\ &\equiv \pi_i^B(p_i^*(E(t^B)), p_j^*(E(t^B)), E(t_i^B)) - E(t_i^B).\end{aligned}\quad (29)$$

The FOC with respect to $E(t_i^B)$ yields

$$\begin{aligned}\frac{\partial (\pi_i^B - E(t_i^B))}{\partial E(t_i^B)} &= \frac{\partial \pi_i^B}{\partial p_i^*} \frac{\partial p_i^*}{\partial E(t_i^B)} + \frac{\partial \pi_i^B}{\partial p_j^*} \frac{\partial p_j^*}{\partial E(t_i^B)} + \frac{\partial \pi_i^B}{\partial E(t_i^B)} - 1 \\ \text{using (28)} &= \frac{\partial \pi_i^B}{\partial p_j^*} \frac{\partial p_j^*}{\partial E(t_i^B)} + \frac{\partial \pi_i^B}{\partial E(t_i^B)} - 1 = 0.\end{aligned}\quad (30)$$

As in the case with managerial incentives, there are four distinct channels through which the manager's expected total compensation affects the principal's objective. First, there is the term $\frac{\partial \pi_i^B}{\partial p_i^*} \frac{\partial p_i^*}{\partial E(t_i^B)}$, which disappears since the firm chooses in a later stage of the game the price that maximizes gross profit. Second, there is the term $\frac{\partial \pi_i^B}{\partial p_j^*} \frac{\partial p_j^*}{\partial E(t_i^B)}$, which captures the extent to which the firm's gross profit is influenced by the impact of its manager's compensation on its rival's price (the "strategic" effect). Third, there is the term $\partial \pi_i^B / \partial E(t_i^B) > 0$, which measures the extent to which the manager's effort reduces the firm's expected marginal cost. Fourth, there is the term -1 , reflecting the direct cost associated with enhancing the manager's compensation.

The following proposition derives the strategic properties of managerial compensation levels:²³

Proposition 3 (Strategic Compensation with Bertrand Competition) *The managerial compensation of firm i responds to a change in the managerial compensation of firm j*

²³For a unique equilibrium of expected total compensation levels $\{E(t_1^B), E(t_2^B)\}$ to exist, we require that $\left| \frac{dE(t_i^B)}{dE(t_j^B)} \right| < 1$. With linear demand, this condition holds for a wide range of parameter values.

as follows:

$$\frac{dE(t_i^B)}{dE(t_j^B)} = - \frac{\frac{\partial^2 \pi_i}{\partial p_j^2} \frac{\partial^2 p_j}{\partial E(t_i) \partial E(t_j)} + \frac{\partial^2 \pi_i}{\partial p_j \partial p_i} \frac{\partial p_i}{\partial E(t_j)} \frac{\partial p_j}{\partial E(t_i)} + \frac{\partial^2 \pi_i}{\partial p_j^2} \frac{\partial p_j}{\partial E(t_j)} \frac{\partial p_j}{\partial E(t_i)}}{\frac{\partial^2 \pi_i}{\partial p_j^2} \frac{\partial^2 p_j}{\partial E(t_i)^2} + \frac{\partial^2 \pi_i}{\partial p_j \partial p_i} \frac{\partial p_i}{\partial E(t_i)} \frac{\partial p_j}{\partial E(t_i)} + \frac{\partial^2 \pi_i}{\partial p_j^2} \left(\frac{\partial p_j}{\partial E(t_i)} \right)^2 + \frac{\partial^2 \pi_i}{\partial E(t_i)^2}}. \quad (31)$$

The rest is the same as the statement in Proposition 1, where the three effects (similar to the three terms in the numerator of (31)) are presented and discussed.

Proof. We totally differentiate (30) with respect to both compensation levels in order to determine the slope of the reaction functions:

$$\left\{ \frac{\partial^2 \pi_i}{\partial p_j^2} \frac{\partial^2 p_j}{\partial E(t_i)^2} + \frac{\partial^2 \pi_i}{\partial p_j \partial p_i} \frac{\partial p_i}{\partial E(t_i)} \frac{\partial p_j}{\partial E(t_i)} + \frac{\partial^2 \pi_i}{\partial p_j^2} \left(\frac{\partial p_j}{\partial E(t_i)} \right)^2 + \frac{\partial^2 \pi_i}{\partial E(t_i)^2} \right\} dE(t_i) + \left\{ \frac{\partial^2 \pi_i}{\partial p_j^2} \frac{\partial^2 p_j}{\partial E(t_i) \partial E(t_j)} + \frac{\partial^2 \pi_i}{\partial p_j \partial p_i} \frac{\partial p_i}{\partial E(t_j)} \frac{\partial p_j}{\partial E(t_i)} + \frac{\partial^2 \pi_i}{\partial p_j^2} \frac{\partial p_j}{\partial E(t_j)} \frac{\partial p_j}{\partial E(t_i)} + \frac{\partial^2 \pi_i}{\partial E(t_i) \partial E(t_j)} \right\} dE(t_j) = 0.$$

The term $\partial^2 \pi_i / (\partial E(t_i) \partial E(t_j))$ is zero since the cost reduction in firm i does not depend on the compensation of the rival firm. The remainder follows as in the proof of Proposition 1.

■

References

- [1] Aggarwal, Rajesh K., and Andrew A. Samwick, 1999a, The other side of the trade-off: The impact of risk on executive compensation, *Journal of Political Economy* 107 (1), 65-105.
- [2] Aggarwal, Rajesh K., and Andrew A. Samwick, 1999b, Executive compensation, strategic competition, and relative performance evaluation: Theory and evidence, *Journal of Finance* 54 (6), 1999-2043.
- [3] Albuquerque, Ana, 2009, Peer firms in relative performance evaluation, *Journal of Accounting and Economics* 48, 69-89.
- [4] Antle, Rick, and Abbie Smith, 1986, An empirical investigation of the relative performance evaluation of corporate executives, *Journal of Accounting Research* 24, 1-39.
- [5] Baggs, Jen, and Jean-Etienne de Bettignies, 2007, Product market competition and agency costs, *Journal of Industrial Economics* 55 (2), 289-323.
- [6] Baker, George P., and Brian J. Hall, 2004, CEO incentives and firm size, *Journal of Labor Economics* 22 (4), 767-798.
- [7] Banker, R., S. Datar, 1989, Sensitivity, precision, and linear aggregation of signals for performance evaluation. *Journal of Accounting Research* 27 (1) 21-39.
- [8] Bizjak, John M., Michael L. Lemmon, and Lalitha Naveen, 2008, Does the use of peer groups contribute to higher pay and less efficient compensation? *Journal of Financial Economics* 90, 152-168.
- [9] Bolton, Patrick, and David Scharfstein, 1990, A theory of predation based on agency problems in financial contracting, *American Economic Review* 80, 93-106.

- [10] Bulow, Jeremy I., John D. Geanakoplos, and Paul D. Klemperer, 1985, Multimarket oligopoly: Strategic substitutes and complements, *Journal of Political Economy* 93 (3), 488-511.
- [11] Bushman, R., R. Indjejikian, 1993, Accounting income, stock price, and managerial compensation. *Journal of Accounting and Economics* 16(1-3) 3-23.
- [12] Bushman, Robert M., Raffi J. Indjejikian, and Abbie Smith, 1996, CEO compensation: The role of individual performance evaluation, *Journal of Accounting and Economics* 21, 161-193.
- [13] Conyon, Martin J., and Kevin J. Murphy, 2000, The prince and the pauper? CEO pay in the United States and United Kingdom, *Economic Journal* 110 (467), F640-F671.
- [14] Core, John, and Wayne Guay, 1999, The use of equity grants to manage optimal equity incentive levels, *Journal of Accounting and Economics* 28 (2), 151-184.
- [15] Core, J., W. Guay, and R. Verrecchia. 2003. Price versus non-price performance measures in optimal CEO compensation contracts. *The Accounting Review* 78 (4) 957-981.
- [16] Core, J., R. W. Holthausen, D. F. Larcker. 1999. Corporate governance, chief executive compensation, and firm performance. *Journal of Financial Economics* 51 371-406.
- [17] Cunat, Vicente, and Maria Guadalupe, 2005, How does product market competition shape incentive contracts? *Journal of the European Economic Association* 3 (5), 1058-1082.
- [18] Cunat, Vicente, and Maria Guadalupe, 2009, Executive compensation and competition in the banking and financial sectors, *Journal of Banking & Finance* 33, 495-504.
- [19] Datar, S., S. Kulp, R. Lambert. 2001. Balancing performance measures. *Journal of Accounting Research* 39 (1) 75-92.

- [20] DeFond, Mark L., and Chul W. Park, 1999, The effect of competition on CEO turnover, *Journal of Accounting and Economics* 27, 35-56.
- [21] Demsetz, Harold, and Kenneth Lehn, 1985, The structure of corporate ownership: Causes and consequences, *Journal of Political Economy* 93, 1155-1177.
- [22] Dutta, S. 2008. Managerial expertise, private information, and pay-performance sensitivity. *Management Science* 54 (3) 429-442.
- [23] Echenique, Federico, 2004, Extensive-form games and strategic complementarities, *Games and Economic Behavior* 46, 348-364.
- [24] Faulkender, Michael, and Jun Yang, 2010, Inside the black box: The role and composition of compensation peer groups, *Journal of Financial Economics*, forthcoming.
- [25] Feltham, G., J. Xie. 1994. Performance measure congruity and diversity in multi-task principal/agent relations. *The Accounting Review* 69 (3) 429-453.
- [26] Fershtman, Chaim, and Kenneth L. Judd, 1987, Equilibrium incentives in oligopoly, *American Economic Review* 77 (5), 927-940.
- [27] Frydman, Carola, and Raven E. Saks, 2010, Executive compensation: A new view from a long-term perspective, 1936-2005, *Review of Financial Studies* 23, 2099-2138.
- [28] Fumas, Vicente Salas, 1992, Relative performance evaluation of management: The effects on industrial competition and risk sharing, *International Journal of Industrial Organization* 10, 473-489.
- [29] Fudenberg, Drew, and Jean Tirole, 1984, The fat-cat effect, the puppy-dog ploy, and the lean and hungry look, *American Economic Review Papers and Proceedings* 74 (2), 361-366.
- [30] Gabaix, Xavier, and Augustin Landier, 2008, Why has CEO pay increased so much? *Quarterly Journal of Economics* 123 (1), 49-100.

- [31] Garen, John E., 1994, Executive compensation and principal-agent theory, *Journal of Political Economy* 102, 1175-1199.
- [32] Gibbons, Robert, and Kevin J. Murphy, 1992, Optimal incentive contracts in the presence of career concerns: Theory and evidence, *Journal of Political Economy* 100, 468-505.
- [33] Hall, Brian J., and Jeffrey B. Liebman, 1998, Are CEOs really paid like bureaucrats? *Quarterly Journal of Economics* 113 (3), 653-691.
- [34] Hart, Oliver D., 1983, The market mechanism as an incentive scheme, *Bell Journal of Economics* 14 (2), 366-382.
- [35] Hayes, Rachel M., and Scott Schaefer, 2009, CEO pay and the Lake Wobegon effect, *Journal of Financial Economics* 94, 280-290.
- [36] Healy, P. 1985. The effect of bonus schemes on accounting decisions. *Journal of Accounting and Economics* 7 85-107.
- [37] Hermalin, Benjamin E., 1992, The effects of competition on executive behavior, *Rand Journal of Economics* 23 (3), 350-365.
- [38] Holmstrom, Bengt, 1979, Moral hazard and observability, *Bell Journal of Economics* 10 (1), 74-91.
- [39] Holmstrom, Bengt, and Paul Milgrom, 1987, Aggregation and linearity in the provision of intertemporal incentives, *Econometrica* 55, 303-328.
- [40] Hubbard, Glenn R., and Darius Palia, 1995, Executive pay and performance: Evidence from the U.S. banking industry, *Journal of Financial Economics* 39, 105-130.
- [41] Ittner, Christopher D., David F. Larcker, and Madhav V. Rajan, 1997, The choice of performance measures in annual bonus contracts, *The Accounting Review* 72 (2), 231-255.

- [42] Janakiraman, Surya, Richard A. Lambert, and David F. Larcker, 1992, An empirical investigation of the relative performance evaluation, *Journal of Accounting Research* 30, 53-69.
- [43] Jensen, Michael, and Kevin J. Murphy, 1990, Performance pay and top management incentives, *Journal of Political Economy* 98, 225-264.
- [44] Jin, Li, 2002, CEO compensation, diversification, and incentives, *Journal of Financial Economics* 66, 29-63.
- [45] Joh, Sung Wook, 1999, Strategic managerial incentive compensation in Japan: Relative performance evaluation and product market competition, *Review of Economics and Statistics* 81, 303-313.
- [46] Karuna, Christo, 2007, Industry product market competition and managerial incentives, *Journal of Accounting and Economics* 43, 275-297.
- [47] Katz, Michael L., 1991, Game-playing agents: Unobservable contracts as precommitments, *Rand Journal of Economics* 22, 307-328.
- [48] Kedia, Simi, 2006, Estimating product market competition: Methodology and application, *Journal of Banking & Finance* 30, 875-894.
- [49] Kreps, David M., and Jose A. Scheinkman, 1983, Quantity precommitment and Bertrand competition yield Cournot outcomes, *Bell Journal of Economics* 14 (2), 326-337.
- [50] Krishnan, Ranjani, 2005, The effect of changes in regulation and competition on firms' demand for accounting information, *Journal of Accounting Research* 80 (1), 269-287.
- [51] Lambert, Richard A., and David F. Larcker, 1987, An analysis of the use of accounting and market measures of performance in executive compensation contracts, *Journal of Accounting Research (Supplement)* 25, 85-125.

- [52] Maksimovic, Vojislav, 1988, Capital structure in repeated oligopolies, *Rand Journal of Economics* 19, 389-407.
- [53] Oyer, Paul, 2004, Why do firms use incentives that have no incentive effects?, *Journal of Finance* 59 (4), 1619-1649.
- [54] Oyer, Paul, and Scott Schaefer, 2005, Why do some firms give stock options to all employees?: An empirical examination of alternative theories, *Journal of Financial Economics* 76, 99-133.
- [55] Prendergast, Canice, 2002, The tenuous trade-off between risk and incentives, *Journal of Political Economy* 110 (5), 1071-1102.
- [56] Raith, Michael, 2003, Competition, risk, and managerial incentives, *American Economic Review* 93 (4), 1425-1436.
- [57] Rajgopal, Shivaram, Terry Shevlin, and Valentina Zamora, 2006, CEOs' outside employment opportunities and the lack of relative performance evaluation in compensation contracts, *Journal of Finance* 61 (4), 1813-1844.
- [58] Rotemberg, Julio, and David Scharfstein, 1990, Shareholder-value maximization and product market competition, *Review of Financial Studies* 3, 367-391.
- [59] Schaefer, Scott, 1998, The dependence of pay-performance sensitivity on the size of the firm, *Review of Economics and Statistics* 80 (3), 436-443.
- [60] Scharfstein, David, 1988, Product-market competition and managerial slack, *Rand Journal of Economics* 19 (1), 147-155.
- [61] Schmidt, Klaus M., 1997, Managerial incentives and product market competition, *Review of Economic Studies* 64 (2), 191-213.
- [62] Sklivas, Steven D., 1987, The strategic choice of managerial incentives, *Rand Journal of Economics* 18 (3), 452-458.

- [63] Sundaram, Anant, Teresa John, and Kose John, 1996, An empirical analysis of strategic competition and firm values: The case of R&D competition, *Journal of Financial Economics* 40, 459-486.
- [64] Sung, J., 2005, Optimal contracts under adverse selection and moral hazard: a continuous time approach, *Review of Financial Studies* 18 (3), 1021-1073.
- [65] Tervio, Marko, 2008, The difference that CEOs make: An assignment model approach, *American Economic Review* 98 (3), 642-668.
- [66] Tirole, Jean, 1988, *The Theory of Industrial Organization*, Cambridge, MA: MIT Press.
- [67] Vickers, John, 1985, Delegation and the theory of the firm, *Economic Journal* 95, 138-147.
- [68] Vives, Xavier, 2009, Strategic complementarity in multi-stage games, *Economic Theory* 40, 151-171.
- [69] Yermack, David, 1995, Do corporations award CEO stock options effectively? *Journal of Financial Economics* 39, 237-269.